

# Stability-Based Controller Design of Cloud Control System With Uncertainties

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**ABSTRACT** A cloud control system (CCS) is inherently uncertain due to the dynamic services and resources in cloud computing. In this paper, an approach of modeling and controller design for CCS is proposed that considers the uncertainties existing in the controlled plant, network, and controller simultaneously; then, a general framework for modeling and controlling uncertain control systems is constructed. First, a typical CCS structure is presented, and the uncertainties in the CCS are analyzed and decomposed. On this basis, a generalized uncertain state-space model is established, which includes the interval controlled plant and the stochastic network, considering the time-delay and packet loss. Meanwhile, the cloud controller model with interval parameters and stochastic time-delay is designed, which includes the state observer and control law. Then, based on the Lyapunov stability theorem and the linear matrix inequality (LMI) method, a stability criterion for obtaining the parameters of the cloud controller is proposed, in which all the results are expressed in the form of the LMI. Finally, simulation results show the effectiveness and generalization performance of the designed cloud controller.

**INDEX TERMS** Cloud control system (CCS), cloud computing, cloud controller, uncertainty analysis, linear matrix inequality (LMI).

## I. INTRODUCTION

The rapid development of information and communication technology and its deep integration with the manufacturing industry have led to major changes in the manufacturing mode, manufacturing process, manufacturing means, ecosystem, etc., and traditional industrial control technologies are facing a new challenge. At present, the conventional control systems, including the integrated control system (ICS), distributed control system (DCS), fieldbus control system (FCS), and networked control system (NCS), have their own advantages and scope of application, but the common problems are shown in their high cost of construction, operation, and maintenance, and the inflexible replacement of the control algorithm [1]–[3]. In recent years, the emergence of cloud computing [4] has brought new ideas to industrial control.

Cloud computing provides dynamically scalable and inexpensive distributed computing capabilities through the network and includes parallel computing, distributed computing, and grid computing [5]. Cloud computing is the result of the hybrid evolution of the concepts of virtualization, utility

computing, infrastructure as a service (IaaS), platform as a service (PaaS), and software as a service (SaaS) [6], [7], which can reach 10 trillion operations per second. In an actual cloud computing system, many computers are connected through the network and virtualized into a configurable shared resource pool including computing, software, data access, and storage services. Then, the computing tasks are loaded into the resource pool to complete the calculation [8]. End-users can use it without knowing the details of actual cloud infrastructures, having the corresponding expertise, or knowing the physical location and specific configuration of the service provider. In this system, computers and other devices provide a service through the network, which enables users to access and use them for resource sharing, software use, and information reading, as if the devices were installed locally. With the continuous improvement of the processing capacity of cloud computing systems, the processing burden of the user terminal can be reduced. Finally, the user terminal can be simplified as a pure input and output device, and the user can purchase services on demand.

In the industrial control scheme, cloud computing is introduced to form the cloud control system (CCS) to realize the interaction between computing and control theory [9]. In the

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cloud, various intelligent learning algorithms, advanced control algorithms, and data-driven modeling methods can be used to realize the autonomous intelligent control of the system while using high-speed communication channels to ensure the real-time control of the system [10]. The control strategy can be provided as the cloud computing service, that is, the idea of “control as a service (CaaS)” [11], [12], which allows the execution of intensive algorithms in the cloud [13]. The most typical feature of CCS is that the controller algorithm is placed in the cloud to form the cloud-based remote control. If the cloud is replaced by a computer, it has a typical NCS structure. Therefore, the CCS will be the next generation of remote control systems after NCS. Due to the virtualization of the controller and the reduction of the hardware and related labor costs, the CCS can significantly reduce the cost and time of the building control system [14] and can flexibly select the control algorithm in the cloud controller according to the different states of different controlled plants to realize “customized” control.

The characteristics of cloud computing, such as virtualization, multi-granularity (node), dynamic scheduling, and soft computing, make it more efficient, open, and scalable. However, there are deficiencies in security, reliability, computing, and communication performance. These issues make cloud computing uncertain [15], adding a new challenge to the design of CCS. Reducing the impact of uncertainty on the performance, reliability, security, and robustness of CCS has become a new research topic. This can be studied from two aspects. First, we can put forward novel dynamic resource management strategies, security protection strategies, cloud infrastructure improvement strategies, and service software optimization from the perspective of cloud computing, and improve the performance of CCS by continuously improving the quality of cloud computing, that is, control of the cloud, which is the main research direction at present [16]. Second, from the control point of view, we can design the control algorithm with enough robustness to compensate for the impact of uncertainty, fully considering various uncertainties (cloud computing, network transmission, etc.), so as to improve the performance of the CCS, that is, control through the cloud. However, there is currently less research in this area.

As an extension of NCS, the concept of cloud control system was discussed in [2], [17], and a rudiment of cloud control system was proposed. Furthermore, the advantages and challenges of cloud control system were introduced in [10], [18]. Mahmoud MS *et al.* proposed the architecture of the industrial automation system based on the cloud [19], as well as the possible problems of network time-delay, data loss, and vulnerability to attack [20]. Some scholars have studied the security problem of the CCS where the physical network between cloud and control system is attacked, and put forward defense strategies to resist these attacks [21]–[23]. In [24], an interactive real-time SCADA platform for the CCS was proposed to receive and monitor scalar and matrix data from different cloud nodes in real time and adjust the parameters of the CCS online. In [25], the parallel

processing performance of the CCS was analyzed and optimized by using the maximum plus algebra method, according to performance indices of the parallel processing system, such as the clock period, throughput, and task completion time. Reference [26] analyzed the network communication requirements of the CCS under different usage backgrounds, and proposed solutions. In terms of cloud control applications, a visual feedback CCS was proposed in [27], using the powerful cloud computing to extract and analyze image features; the authors also analyzed the time-delay caused by the addition of cloud characteristics and proposed a switching gain control strategy for the influence of cloud characteristics. In [28], [29], a new virtual cloud laboratory education platform was proposed; it used a cloud storage platform to share learning materials and enable students to remotely control the virtual machine to perform experimental tasks. The intelligent transportation cyber-physical CCS was designed in [30], [31]. It can accurately predict short-term traffic flow and road congestion, and then obtain a real-time traffic flow control strategy through an intelligent optimal scheduling algorithm in the cloud. A cloud robot architecture was proposed in [32], enabling robots to share computing resources, information, and data with each other in the shared resource pool in the cloud, and to access new knowledge and skills. In [33], preliminary work of low-level motion control of a desktop 3D printer from the cloud was introduced. Through the cloud control algorithm provided by CaaS, the control performance of desktop 3D printer can be significantly improved at a low cost. Ultimately, the research and applications of the CCS are in preliminary stages. In [34], we proposed that the uncertainty of cloud computing would cause uncertainty of the cloud controller and affect the stability of the system, and used the Lyapunov stability theory [35]–[37] to design the controller to make the system stable. This paper focuses on the modeling and controller design of the discrete CCS with various uncertainties from the control point of view.

The contribution of this paper is mainly reflected in three aspects. First, we propose the basic framework of the CCS and the uncertainty decomposition strategy to simplify the modeling and controller design of the CCS. Second, the controller uncertainty is further elaborated and modeled according to the characteristics of the cloud control. Compared with the existing control system, it is a novel approach to controller design. Third, we propose a unified control system design framework with uncertainties including the controlled plant, network, and cloud controller; then, the corresponding mathematical model is established, and the controller is designed based on the stability principle.

The remainder of this paper is organized as follows. Section II presents a typical structure of the CCS and the uncertainty of CCS is analyzed and decomposed. Then in Section III, the model of uncertain CCS is given, considering the uncertainties existing in the controlled plant, network and cloud controller. In Section IV, the main results including stability analysis and controller parameter solution are presented. Section V conducts the CCS simulations for

two typical controlled plants, demonstrating the effectiveness and generalization of the proposed method, and Section VI concludes this paper.

*Notations:* Throughout this paper,  $R^n$  denotes  $n$ -dimensional Euclidean space,  $R^{n \times m}$  is the set of all  $n \times m$  real matrices,  $I$  denotes identity matrix of appropriate dimension, and “\*” denotes the transposed matrices in the symmetric positions. The notations  $X > Y$  and  $X \geq Y$ , where  $X$  and  $Y$  are matrices of the same dimensions, mean that the matrix  $(X - Y)$  is positive definite and positive semi-definite, respectively. The interval matrix  $[\underline{A}, \bar{A}]$  is defined as  $[\underline{A}, \bar{A}] = \{A = [a_{ij}]; \underline{a}_{ij} \leq a_{ij} \leq \bar{a}_{ij}, 1 \leq i, j \leq n\}$ , where  $\underline{A} = [\underline{a}_{ij}]_{n \times n}$ ,  $\bar{A} = [\bar{a}_{ij}]_{n \times n}$ , and satisfies  $\underline{a}_{ij} \leq \bar{a}_{ij}$ .  $\Pr\{\cdot\}$  means mathematical probability,  $E\{\cdot\}$  stands for mathematical expectation and  $Var\{\cdot\}$  denotes the variance.

**II. TYPICAL STRUCTURE AND UNCERTAIN DECOMPOSITION OF THE CCS**

In this section, first we introduce the basic concept and typical structure of CCS. Then, the uncertainties in the CCS are analyzed, and a decomposition strategy is proposed.

**A. CLOUD CONTROL CONCEPT AND TYPICAL STRUCTURE**

Reviewing the conventional control system design and the various control systems used, that is, from ICS, DCS, FCS to NCS, the software and hardware configuration are mainly around the core of “controller”. The engineer’s focus is the computer which runs various control algorithms, while the controlled plant (or process) is generally placed at the far end. However, the core idea based on cloud computing is to design the control system around the controlled plant (or process). Engineers can put various controllers (control algorithm, optimization algorithm, etc.) in the distant “cloud” to form a cloud controller [38], while the controlled plants only need to send the real-time detection signals and receive remote control signals through the highspeed network. The engineers can monitor the running status of the controlled plant in real time through a mobile device (such as a mobile phone) or a computer.

The CCS is structured as deep integration of cloud computing and a cyber-physical system. In [9], [14], a cloud-based automation architecture is proposed, which essentially relaxes the existing systems layers and reflects the relationship between each component and the layers in the industrial automation system. However, the CCS is an extension of the NCS and a new generation computer control system in the future. Therefore, we simplify and abstract the CCS as the basic structure of the computer control system from the control point of view, which divides the CCS into four parts, including controlled plant, network channel, cloud controller, and monitoring terminal as shown in Fig. 1. Compared with [9], [14], we can use the existing control theory to understand and analyze it more simply and easily.

The database, control algorithm library, optimized algorithm library, etc., are constructed on a cloud server, connected to each other and managed through server software

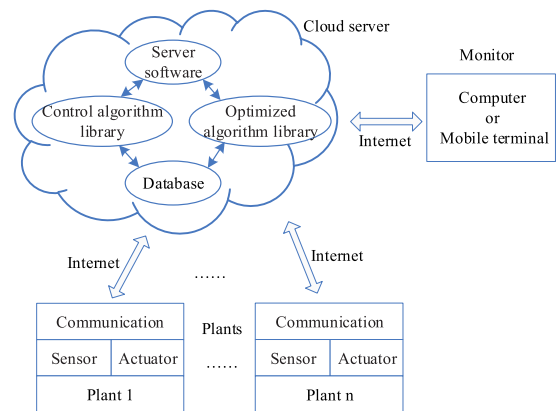


FIGURE 1. General structure of the CCS.

in the cloud. In the generalized controlled plant part, the top layer is the Internet communication interface, while the middle layer includes the sensor and actuator, and the bottom layer is the controlled plant itself. Each state variable of the bottom controlled plant is acquired by the sensor in real-time and sent to the cloud server; the actuator receives the control order from the cloud and then performs real-time control on each operating variable. For supervising the running state of the controlled plant in real-time, the monitor can be a mobile device terminal (such as a mobile phone) or a computer. The network is the Internet, connecting the cloud and the local controlled plants as well as the monitor and exchanging information among them.

This structure can effectively overcome problems such as the inflexible update and replacement of control algorithms and more requirements on system hardware, making the control system design more flexible and convenient. Without increasing the hardware cost, the cloud can identify the different characteristics of the controlled plant model according to a large amount of data about the controlled plant and the decision information obtained from big data mining in the cloud, so as to automatically select the appropriate control algorithm for engineers from the control algorithm library and optimization algorithm library. Engineers can also manually select the appropriate control algorithm or upload the control algorithm to the cloud according to the actual operation of the controlled plant in the industrial field; In this way, “customized” control is realized.

However, due to the uncertainties existing in the controlled plant, network channel, and cloud computing, the CCS is actually an uncertain system. The modeling and control of CCS are more complex and challenging due to the existence and high complexity of various uncertainties, compared with the previous control system. Next, we will analyze the uncertainties in CCS and decompose them.

**B. UNCERTAINTY ANALYSIS OF CONTROLLED PLANT AND NETWORK**

Due to the influence of internal parameter perturbation, parameter measurement error, identification error, and other

factors, the parameters of the actual controlled plant in the industry are often uncertain. In fact, we can say that most control systems are uncertain ones. Although uncertainty does not often change the system structure, its existence degrades the performance of the controller designed on the nominal system and can cause system instability. In most cases, the upper and lower bounds of parameters are easy to know, and therefore the interval number can be used to conveniently express the uncertain parameters of some control systems. In fact, considering the uncertainty of the controlled plant in the CCS, the designed controller will have a wider range of applications.

The cloud controller must communicate with the sensor and the actuator through the network, and the communication network has transmission time-delay, packet loss, timing disorder, and other uncertainties, due to congestion, equipment failure, network load [39], and other reasons, which will affect the performance and stability of the CCS. Besides, there are two different features in the network of the CCS. First, when modeling and controlling the control system, we must consider bilateral delay; however, in NCS, we can sometimes only consider the unilateral delay [40]–[42]. Even if the bilateral delay is considered in NCS [43]–[45], the network delay in CCS may show different characteristics due to the uncertainties of cloud computing itself. Second, due to the dynamic scheduling of resources, the uncertainty of cloud computing itself often leads to the time-related uncertainty of the cloud controller itself. This leads to the influence of the forward and feedback channel time-delays being different, and therefore, they cannot be simply combined into a single time-delay like in the NCS [46], [47].

### C. CLOUD UNCERTAINTY ANALYSIS

As aforementioned, cloud computing also has many uncertainties due to dynamic resource scheduling [48], such as random computing delay, packet loss, and timing chaos. The existence of these uncertainties will cause the uncertainties of the cloud controller, among which the impact of time-delay on the cloud controller is most prominent.

The cloud controller is put in the cloud far away from the physical system, and due to load balancing, distributed computing, massive data processing, and other requirements, the data transmission delay between nodes and calculated delay of each node in the cloud [49] are larger than that of the NCS, and their randomness is more complex. At this time, the computing time-delay of the cloud controller cannot be simply included in the network time-delay, nor can it be ignored.

Although the reliability of the cloud is much greater than that of the network in general, it is inevitable that network congestion, connection interruptions, and channel interference will occur in the process of receiving and sending data packets, resulting in data packet loss. The communication information between nodes includes not only the data information required by the relevant calculation, but also the controller parameters, structure, control variables, and other



FIGURE 2. Uncertainties decomposition diagram of the CCS.

information. Therefore, the packet loss at the cloud will not only cause the loss of the relevant sampling data, but also cause the loss of the relevant information of the controller, which is different from the packet loss at the network, resulting in the uncertainty of the controller itself.

In addition, external attacks or interference may also cause cloud data to be leaked or tampered with artificially [50], which means the parameters and structure of various control algorithms placed in the cloud are changed, reducing the control effect without the cloud monitoring system noticing. This requires the cloud controller to have a certain degree of non-vulnerability so that the controller can hold the system stable when it is disturbed.

### D. DECOMPOSITION STRATEGY OF CCS UNCERTAINTY

The CCS can be considered as the integration of cloud computing and the NCS, including all the characteristics of the NCS. The NCS itself has uncertainties of the network and the controlled plant. The CCS further increases the uncertainty by introducing cloud computing. The mixture of many uncertainties makes the modeling and control of the CCS more complex and difficult.

Therefore, in order to facilitate the analysis, this paper decomposes the uncertainties of the CCS, as shown in Fig. 2. It is considered that there are mainly three kinds of uncertainties in the generalized CCS: cloud controller uncertainty, network uncertainty, and controlled plant uncertainty, which together constitute the uncertainty of the whole system.

The advantage of this decomposition strategy is that it can make full use of the existing theoretical results of the NCS (including the network side and the controlled plant side) and concentrate on the uncertainty analysis of the cloud controller. On this basis, the three uncertainty models can be effectively combined according to some principles, thereby simplifying the complexity and reducing the difficulty of modeling the CCS with uncertainties.

## III. CCS MODEL

In this section, the state-space model of a generalized uncertain controlled plant with the network delay and packet loss is established, and the cloud uncertainty is considered to obtain the cloud controller model including an observer with uncertain parameters and control law. Finally, the state equation of the closed-loop CCS is constructed based on these two models.

### A. UNCERTAIN PARAMETERS SETTING

The structure of the discrete CCS considered in this paper is shown in Fig. 3. In the CCS, the time-delays of network channel and cloud controller are time-varying,



$$E_1 = [I_1, \dots, I_n, \dots, I_1, \dots, I_n]_{n^2 \times n}^T, \quad (4b)$$

$$D_2 = [b_{1,11}^* I_1, \dots, b_{1,1m}^* I_1, \dots, b_{1,n1}^* I_n, \dots, b_{1,nn}^* I_n]_{n \times nm}, \quad (4c)$$

$$E_2 = [I_1, \dots, I_n, \dots, I_1, \dots, I_n]_{nm \times n}^T, \quad (4d)$$

where  $I_i$  denotes the  $i$ th column vector of the identity matrix, and  $F_1$  and  $F_2$  are the time-varying diagonal matrices with appropriate dimensions, and the absolute values of their diagonal elements are not larger than 1.

In the control system, all or part of the state cannot be directly measured, and the state observer can be described as

$$\begin{cases} \hat{x}_{k+1} = A_2 \hat{x}_k + B_2 \bar{u}_k + L (\bar{y}_k - \alpha_k \hat{y}_{k-\tau_k^{sc}}) \\ \hat{y}_k = C \hat{x}_k, \end{cases} \quad (5)$$

where  $\hat{x}_k$  is the state vector of the observer,  $\hat{y}_k$  is the output vector of the observer,  $L$  is the observer gain matrix,  $\bar{y}_k$  and  $\bar{u}_k$  are system output and control input vectors sent to the observer, respectively.  $\alpha_k \hat{y}_{k-\tau_k^{sc}}$  is the output value of the observer corresponding to  $\bar{y}_k$ , which is used to correct the state reconstruction. In addition to time-delay, other uncertain factors, such as packet loss and external disturbance in cloud computing, may change the parameters of cloud controller. Therefore, it is assumed that  $A_2 \in R^{n \times n}$ ,  $B_2 \in R^{n \times m}$  are the interval parameter matrices with the appropriate dimensions, whose median values are the same as that of the nominal system, but the widths are different, that is,  $A_2 = [\underline{A}_2, \bar{A}_2]$ ,  $B_2 = [\underline{B}_2, \bar{B}_2]$ . Similarly, it can be obtained that

$$A_0 = \frac{1}{2}(\underline{A}_2 + \bar{A}_2) = \frac{1}{2}(\underline{A}_1 + \bar{A}_1), \quad (6a)$$

$$B_0 = \frac{1}{2}(\underline{B}_2 + \bar{B}_2) = \frac{1}{2}(\underline{B}_1 + \bar{B}_1), \quad (6b)$$

$$\Delta A_2 = \frac{1}{2}(\bar{A}_2 - \underline{A}_2) = (a_{2,ij}^*)_{n \times n}, \quad (6c)$$

$$\Delta B_2 = \frac{1}{2}(\bar{B}_2 - \underline{B}_2) = (b_{2,ik}^*)_{n \times m}. \quad (6d)$$

Then,  $A_2$  and  $B_2$  can be written as  $A_2 = A_0 + D_3 F_3 E_3$ ,  $B_2 = B_0 + D_4 F_4 E_4$ , where

$$D_3 = [a_{2,11}^* I_1, \dots, a_{2,1n}^* I_1, \dots, a_{2,n1}^* I_n, \dots, a_{2,nn}^* I_n]_{n \times n^2}, \quad (7a)$$

$$E_3 = [I_1, \dots, I_n, \dots, I_1, \dots, I_n]_{n^2 \times n}^T, \quad (7b)$$

$$D_4 = [b_{2,11}^* I_1, \dots, b_{2,1m}^* I_1, \dots, b_{2,n1}^* I_n, \dots, b_{2,nn}^* I_n]_{n \times nm}, \quad (7c)$$

$$E_4 = [I_1, \dots, I_n, \dots, I_1, \dots, I_n]_{nm \times n}^T, \quad (7d)$$

where  $I_i$  denotes the  $i$ th column vector of the identity matrix, and  $F_3$  and  $F_4$  are the time-varying diagonal matrices with appropriate dimensions, and the absolute values of their diagonal elements are not larger than 1.

The output of the controller considering the time-delay of the cloud controller can be expressed as

$$\bar{u}_k = K \hat{x}_{k-\tau_k^c} \quad (8)$$

where  $K$  is the gain matrix of the control law.

Considering network time-delay and packet loss, the system output sent to observer and control input received by actuator can be expressed as

$$\bar{y} = \alpha_k y_{k-\tau_k^{sc}}, \quad (9)$$

$$u_k = \beta_k \bar{u}_{k-\tau_k^{ca}} = \beta_k K \hat{x}_{k-\tau_k^{ca}-\tau_k^c}. \quad (10)$$

State estimation error and augmented matrix are respectively defined as

$$e_k = x_k - \hat{x}_k, \quad (11)$$

$$\xi_k = \begin{bmatrix} x_k^T \\ e_k^T \end{bmatrix}^T. \quad (12)$$

The state equation of the closed-loop CCS can be obtained from (2) - (12).

$$\xi_{k+1} = \tilde{A} \xi_k + \alpha_k I_1 L \tilde{C} \xi_{k-\phi_k} + \tilde{B} K I_2 \xi_{k-\phi_k} + \beta_k \hat{B} K I_3 \xi_{k-\psi_k} \quad (13)$$

where  $\tilde{A} = \begin{bmatrix} A_1 & 0 \\ A_1 - A_2 & A_2 \end{bmatrix}$ ,  $I_1 = \begin{bmatrix} 0 \\ I \end{bmatrix}$ ,  $\tilde{C} = [0 \ C]$ ,  $\tilde{B} = \begin{bmatrix} 0 \\ B_2 \end{bmatrix}$ ,  $I_2 = [-I \ I]$ ,  $\hat{B} = \begin{bmatrix} B_1 \\ B_1 \end{bmatrix}$ ,  $I_3 = [I \ -I]$ ,  $\phi_k = \tau_k^{sc}$ ,  $\varphi_k = \tau_k^c$ ,  $\psi_k = \tau_k^{ca} + \tau_k^c$ .

Because  $A_1$ ,  $B_1$ ,  $A_2$ , and  $B_2$  are interval matrices,  $\tilde{A}$ ,  $\tilde{B}$ , and  $\hat{B}$  can be expressed as

$$\begin{aligned} \tilde{A} &= \tilde{A}_0 + \tilde{D}_1 \tilde{F}_1 \tilde{E}_1, & \tilde{B} &= \tilde{B}_0 + \tilde{D}_2 \tilde{F}_2 \tilde{E}_2, \\ \hat{B} &= \hat{B}_0 + \tilde{D}_3 \tilde{F}_3 \tilde{E}_3, \end{aligned} \quad (14)$$

where  $\tilde{A}_0 = \begin{bmatrix} A_0 & 0 \\ 0 & A_0 \end{bmatrix}$ ,  $\tilde{D}_1 = \begin{bmatrix} D_1 & 0 \\ D_1 & D_3 \end{bmatrix}$ ,  $\tilde{F}_1 = \begin{bmatrix} F_1 & 0 \\ 0 & F_3 \end{bmatrix}$ ,  $\tilde{E}_1 = \begin{bmatrix} E_1 & 0 \\ -E_3 & E_3 \end{bmatrix}$ ,  $\tilde{B}_0 = \begin{bmatrix} 0 \\ B_0 \end{bmatrix}$ ,  $\tilde{D}_2 = \begin{bmatrix} 0 \\ D_4 \end{bmatrix}$ ,  $\tilde{F}_2 = \begin{bmatrix} 0 \\ D_4 \end{bmatrix}$ ,  $\tilde{E}_2 = E_4$ ,  $\hat{B}_0 = \begin{bmatrix} B_0 \\ B_0 \end{bmatrix}$ ,  $\tilde{D}_3 = \begin{bmatrix} D_2 \\ D_2 \end{bmatrix}$ ,  $\tilde{F}_3 = F_2$ ,  $\tilde{E}_3 = E_2$ .

## IV. MAIN RESULTS

In this section, the main results of this paper are presented. Firstly, the following definitions and lemmas are given. Then, the theorem about the stability criteria of the CCS is given on the basis of the Lyapunov theorem. And the linear matrix inequality (LMI) method is adopted to obtain the parameters of the cloud controller.

### A. RELATED DEFINITIONS AND LEMMAS

*Definition 1* ([52]): For any initial system state  $\xi_0$  and initial time-delay mode  $\phi_0 \in \Omega$ ,  $\varphi_0 \in \Lambda$ ,  $\psi_0 \in \Upsilon$ , if there exists a positive definite matrix  $W$ , such that

$$E \left\{ \sum_{k=0}^{\infty} \|\xi_k\|^2 \mid \phi_0, \varphi_0, \psi_0 \right\} < \xi_0^T W \xi_0 \quad (15)$$

the closed-loop system (13) is said to be stochastically stable.

*Lemma 1* ([53]): For any positive definite matrix  $H$  and two scalar  $\theta$ ,  $\theta_0$  satisfying  $\theta > \theta_0 \geq 1$ , the following formula always holds:

$$\left( \sum_{\rho=\theta_0}^{\theta} v_{\rho} \right)^T H \sum_{\rho=\theta_0}^{\theta} v_{\rho} \leq (\theta - \theta_0 + 1) \sum_{\rho=\theta_0}^{\theta} v_{\rho}^T H v_{\rho} \quad (16)$$

*Lemma 2* ([54]): Given real matrices  $M = M^T$ ,  $H$  and  $E$  with  $F(t)$  satisfying  $F(t)F^T(t) < I$ , then  $M + HFE + E^T F^T H^T < 0$ , if and only if there exists a positive scalar  $\varepsilon$  such that

$$M + \varepsilon HH^T + \varepsilon^{-1} E^T E < 0 \quad (17)$$

or equivalently

$$\begin{bmatrix} M & \varepsilon H & E^T \\ \varepsilon H^T & -\varepsilon I & 0 \\ E & 0 & -\varepsilon I \end{bmatrix} < 0 \quad (18)$$

**B. STABILITY ANALYSIS**

In this subsection, a stability theorem will be stated, which gives a sufficient condition for the stochastic stability of the closed-loop uncertain CCS.

*Theorem 1:* Under the presented control law (8), the CCS (13) with uncertainties is stochastically stable if for given scalars  $0 \leq \bar{\alpha} \leq 1, 0 \leq \bar{\beta} \leq 1$ , there exist matrices  $K, L$  with proper dimensions and symmetric positive definite matrices  $R_{acm} > 0, R_{bdn} > 0, P_1 > 0, P_2 > 0, P_3 > 0, P_4 > 0, P_5 > 0, P_6 > 0, Q_1 > 0, Q_2 > 0, Q_3 > 0$ , such that the following matrix inequality (19) holds for all  $a, b \in \Omega, c, d \in \Lambda, m, n \in \Upsilon$ .

$$\Gamma \triangleq \begin{bmatrix} \Gamma_{11} & * & * & * & * & * & * \\ \Gamma_{21} & \Gamma_{22} & * & * & * & * & * \\ \Gamma_{31} & \Gamma_{32} & \Gamma_{33} & * & * & * & * \\ \Gamma_{41} & \Gamma_{42} & \Gamma_{43} & \Gamma_{44} & * & * & * \\ 0 & Q_1 & 0 & 0 & -P_1 - Q_1 & * & * \\ 0 & 0 & Q_2 & 0 & 0 & -P_2 - Q_2 & * \\ 0 & 0 & 0 & Q_3 & 0 & 0 & -P_3 - Q_3 \end{bmatrix} < 0 \quad (19)$$

where

$$\begin{aligned} \Gamma_{11} &= \tilde{A}^T \bar{R}_{bdn} \tilde{A} - R_{acm} + P_1 + P_2 + P_3 + (\phi_M + 2)P_4 \\ &\quad + (\varphi_M + 2)P_5 + (\psi_M + 2)P_6 + \phi_M^2 (\tilde{A} - I)^T Q_1 (\tilde{A} - I) \\ &\quad + \varphi_M^2 (\tilde{A} - I)^T Q_2 (\tilde{A} - I) + \psi_M^2 (\tilde{A} - I)^T Q_3 (\tilde{A} - I) \\ &\quad - Q_1 - Q_2 - Q_3 \end{aligned}$$

$$\begin{aligned} \Gamma_{21} &= (\bar{\alpha} I_1 L \tilde{C})^T \bar{R}_{bdn} \tilde{A} + \phi_M^2 (\bar{\alpha} I_1 L \tilde{C})^T Q_1 (\tilde{A} - I) \\ &\quad + \varphi_M^2 (\bar{\alpha} I_1 L \tilde{C})^T Q_2 (\tilde{A} - I) \\ &\quad + \psi_M^2 (\bar{\alpha} I_1 L \tilde{C})^T Q_3 (\tilde{A} - I) + Q_1 \end{aligned}$$

$$\begin{aligned} \Gamma_{22} &= (\alpha_1^2 + \bar{\alpha}^2) (I_1 L \tilde{C})^T \bar{R}_{bdn} I_1 L \tilde{C} \\ &\quad - P_4 + \phi_M^2 (\alpha_1^2 + \bar{\alpha}^2) (I_1 L \tilde{C})^T Q_1 I_1 L \tilde{C} \\ &\quad + \varphi_M^2 (\alpha_1^2 + \bar{\alpha}^2) (I_1 L \tilde{C})^T Q_2 I_1 L \tilde{C} \\ &\quad + \psi_M^2 (\alpha_1^2 + \bar{\alpha}^2) (I_1 L \tilde{C})^T Q_3 I_1 L \tilde{C} - 2Q_1 \end{aligned}$$

$$\begin{aligned} \Gamma_{31} &= (\tilde{B} K I_2)^T \bar{R}_{bdn} \tilde{A} + \phi_M^2 (\tilde{B} K I_2)^T Q_1 (\tilde{A} - I) \\ &\quad + \varphi_M^2 (\tilde{B} K I_2)^T Q_2 (\tilde{A} - I) \\ &\quad + \psi_M^2 (\tilde{B} K I_2)^T Q_3 (\tilde{A} - I) + Q_2 \end{aligned}$$

$$\begin{aligned} \Gamma_{32} &= (\tilde{B} K I_2)^T \bar{R}_{bdn} \bar{\alpha} I_1 L \tilde{C} + \phi_M^2 (\tilde{B} K I_2)^T Q_1 \bar{\alpha} I_1 L \tilde{C} \\ &\quad + \varphi_M^2 (\tilde{B} K I_2)^T Q_2 \bar{\alpha} I_1 L \tilde{C} + \psi_M^2 (\tilde{B} K I_2)^T Q_3 \bar{\alpha} I_1 L \tilde{C} \end{aligned}$$

$$\begin{aligned} \Gamma_{33} &= (\tilde{B} K I_2)^T \bar{R}_{bdn} \tilde{B} K I_2 - P_5 + \phi_M^2 (\tilde{B} K I_2)^T Q_1 \tilde{B} K I_2 \\ &\quad + \varphi_M^2 (\tilde{B} K I_2)^T Q_2 \tilde{B} K I_2 + \psi_M^2 (\tilde{B} K I_2)^T Q_3 \tilde{B} K I_2 - 2Q_2 \end{aligned}$$

$$\begin{aligned} \Gamma_{41} &= (\bar{\beta} \hat{B} K I_3)^T \bar{R}_{bdn} \tilde{A} + \phi_M^2 (\bar{\beta} \hat{B} K I_3)^T Q_1 (\tilde{A} - I) \\ &\quad + \varphi_M^2 (\bar{\beta} \hat{B} K I_3)^T Q_2 (\tilde{A} - I) \\ &\quad + \psi_M^2 (\bar{\beta} \hat{B} K I_3)^T Q_3 (\tilde{A} - I) + Q_3 \end{aligned}$$

$$\begin{aligned} \Gamma_{42} &= (\bar{\beta} \hat{B} K I_3)^T \bar{R}_{bdn} \bar{\alpha} I_1 L \tilde{C} \\ &\quad + \phi_M^2 (\bar{\beta} \hat{B} K I_3)^T Q_1 \bar{\alpha} I_1 L \tilde{C} \\ &\quad + \varphi_M^2 (\bar{\beta} \hat{B} K I_3)^T Q_2 \bar{\alpha} I_1 L \tilde{C} \\ &\quad + \psi_M^2 (\bar{\beta} \hat{B} K I_3)^T Q_3 \bar{\alpha} I_1 L \tilde{C} \end{aligned}$$

$$\begin{aligned} \Gamma_{43} &= (\bar{\beta} \hat{B} K I_3)^T \bar{R}_{bdn} \tilde{B} K I_2 + \phi_M^2 (\bar{\beta} \hat{B} K I_3)^T Q_1 \tilde{B} K I_2 \\ &\quad + \varphi_M^2 (\bar{\beta} \hat{B} K I_3)^T Q_2 \tilde{B} K I_2 + \psi_M^2 (\bar{\beta} \hat{B} K I_3)^T Q_3 \tilde{B} K I_2 \end{aligned}$$

$$\begin{aligned} \Gamma_{44} &= (\beta_1^2 + \bar{\beta}^2) (\hat{B} K I_3)^T \bar{R}_{bdn} \hat{B} K I_3 - P_6 \\ &\quad + \phi_M^2 (\beta_1^2 + \bar{\beta}^2) (\hat{B} K I_3)^T Q_1 \hat{B} K I_3 \\ &\quad + \varphi_M^2 (\beta_1^2 + \bar{\beta}^2) (\hat{B} K I_3)^T Q_2 \hat{B} K I_3 \\ &\quad + \psi_M^2 (\beta_1^2 + \bar{\beta}^2) (\hat{B} K I_3)^T Q_3 \hat{B} K I_3 - 2Q_3 \end{aligned}$$

$$\bar{R}_{bdn} = \sum_{b=0}^{\phi_M} \sum_{d=0}^{\varphi_M} \sum_{n=0}^{\psi_M} \mu_{ab} \nu_{cd} \sigma_{mn} R_{bdn}.$$

*Proof:* As shown in Appendix A.

**C. SOLUTION OF CONTROLLER PARAMETERS**

The matrix inequality in (19) is bilinear, which needs to be converted into LMI to obtain the control law gain matrix  $K$  and the observer gain matrix  $L$ , thus, Theorem 2 is given.

*Theorem 2:* Under the presented control law (8), the CCS (13) with uncertainties is stochastically stable if for given scalars  $0 \leq \bar{\alpha} \leq 1, 0 \leq \bar{\beta} \leq 1$ , there exist matrices  $K, L$  with proper dimensions, symmetric matrices  $R_{acm} > 0, S_{bdn} > 0, P_1 > 0, P_2 > 0, P_3 > 0, P_4 > 0, P_5 > 0, P_6 > 0, Q_1 > 0, Q_2 > 0, Q_3 > 0$  and real scalars  $\varepsilon_1, \varepsilon_2, \varepsilon_3, \varepsilon_4, \varepsilon_5, \varepsilon_6, \varepsilon_7, \varepsilon_8 > 0$ , such that the following linear matrix inequality (30) - (37) hold for all  $a, b \in \Omega, c, d \in \Lambda, m, n \in \Upsilon$ .

$$\begin{bmatrix} \mu \nu \sigma \Xi_0 & * & * & * & * & * \\ X_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} & \Psi_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} & * & * & * & * \\ \varepsilon_1 \tilde{D}^T & 0 & -\varepsilon_1 I & * & * & * \\ 0 & \varepsilon_1 \tilde{D}^T \Omega_k^a \Lambda_k^c \Upsilon_k^m & 0 & -\varepsilon_1 I & * & * \\ \tilde{E} & 0 & 0 & 0 & -\varepsilon_1 I & * \\ \tilde{E} \Omega_k^a \Lambda_k^c \Upsilon_k^m & 0 & 0 & 0 & 0 & -\varepsilon_1 I \end{bmatrix} < 0 \quad (30)$$

$$\begin{bmatrix} \mu \sigma \Xi_0 & * & * & * & * & * \\ X_{\Omega_k^a \Lambda_{uk}^c \Upsilon_k^m} & \Psi_{\Omega_k^a \Lambda_{uk}^c \Upsilon_k^m} & * & * & * & * \\ \varepsilon_2 \tilde{D}^T & 0 & -\varepsilon_2 I & * & * & * \\ 0 & \varepsilon_2 \tilde{D}^T \Omega_k^a \Lambda_{uk}^c \Upsilon_k^m & 0 & -\varepsilon_2 I & * & * \\ \tilde{E} & 0 & 0 & 0 & -\varepsilon_2 I & * \\ \tilde{E} \Omega_k^a \Lambda_{uk}^c \Upsilon_k^m & 0 & 0 & 0 & 0 & -\varepsilon_2 I \end{bmatrix} < 0 \quad (31)$$

$\forall d \in \Lambda_{uk}^c$

$$\begin{bmatrix} \mu\nu\Xi_0 & * & * & * & * & * \\ X_{\Omega_k^a\Lambda_k^c\Upsilon_{uk}^m} & \Psi_{\Omega_k^a\Lambda_k^c\Upsilon_{uk}^m} & * & * & * & * \\ \varepsilon_3\tilde{D}^T & 0 & -\varepsilon_3I & * & * & * \\ 0 & \varepsilon_3\tilde{D}_{\Omega_k^a\Lambda_k^c\Upsilon_{uk}^m}^T & 0 & -\varepsilon_3I & * & * \\ \tilde{E} & 0 & 0 & 0 & -\varepsilon_3I & * \\ \tilde{E}_{\Omega_k^a\Lambda_k^c\Upsilon_{uk}^m} & 0 & 0 & 0 & 0 & -\varepsilon_3I \end{bmatrix} < 0$$

(32)

$$\begin{bmatrix} \mu\Xi_0 & * & * & * & * & * \\ X_{\Omega_k^a\Lambda_k^c\Upsilon_{uk}^m} & \Psi_{\Omega_k^a\Lambda_k^c\Upsilon_{uk}^m} & * & * & * & * \\ \varepsilon_4\tilde{D}^T & 0 & -\varepsilon_4I & * & * & * \\ 0 & \varepsilon_4\tilde{D}_{\Omega_k^a\Lambda_k^c\Upsilon_{uk}^m}^T & 0 & -\varepsilon_4I & * & * \\ \tilde{E} & 0 & 0 & 0 & -\varepsilon_4I & * \\ \tilde{E}_{\Omega_k^a\Lambda_k^c\Upsilon_{uk}^m} & 0 & 0 & 0 & 0 & -\varepsilon_4I \end{bmatrix} < 0$$

(33)

$$\begin{bmatrix} \nu\sigma\Xi_0 & * & * & * & * & * \\ X_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m} & \Psi_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m} & * & * & * & * \\ \varepsilon_5\tilde{D}^T & 0 & -\varepsilon_5I & * & * & * \\ 0 & \varepsilon_5\tilde{D}_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m}^T & 0 & -\varepsilon_5I & * & * \\ \tilde{E} & 0 & 0 & 0 & -\varepsilon_5I & * \\ \tilde{E}_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m} & 0 & 0 & 0 & 0 & -\varepsilon_5I \end{bmatrix} < 0$$

(34)

$$\begin{bmatrix} \nu\Xi_0 & * & * & * & * & * \\ X_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m} & \Psi_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m} & * & * & * & * \\ \varepsilon_6\tilde{D}^T & 0 & -\varepsilon_6I & * & * & * \\ 0 & \varepsilon_6\tilde{D}_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m}^T & 0 & -\varepsilon_6I & * & * \\ \tilde{E} & 0 & 0 & 0 & -\varepsilon_6I & * \\ \tilde{E}_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m} & 0 & 0 & 0 & 0 & -\varepsilon_6I \end{bmatrix} < 0$$

(35)

$$\begin{bmatrix} \sigma\Xi_0 & * & * & * & * & * \\ X_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m} & \Psi_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m} & * & * & * & * \\ \varepsilon_7\tilde{D}^T & 0 & -\varepsilon_7I & * & * & * \\ 0 & \varepsilon_7\tilde{D}_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m}^T & 0 & -\varepsilon_7I & * & * \\ \tilde{E} & 0 & 0 & 0 & -\varepsilon_7I & * \\ \tilde{E}_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m} & 0 & 0 & 0 & 0 & -\varepsilon_7I \end{bmatrix} < 0$$

(36)

$$\begin{bmatrix} \Xi_0 & * & * & * & * & * \\ X_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m} & \Psi_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m} & * & * & * & * \\ \varepsilon_8\tilde{D}^T & 0 & -\varepsilon_8I & * & * & * \\ 0 & \varepsilon_8\tilde{D}_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m}^T & 0 & -\varepsilon_8I & * & * \\ \tilde{E} & 0 & 0 & 0 & -\varepsilon_8I & * \\ \tilde{E}_{\Omega_{uk}^a\Lambda_{uk}^c\Upsilon_{uk}^m} & 0 & 0 & 0 & 0 & -\varepsilon_8I \end{bmatrix} < 0$$

(37)

where the definition of parameters in (30)-(37) is given in Appendix B.

*Proof:* Equation (19) can be converted to (38).

$$\Gamma = \Xi_{11} - \Xi_{21}^T \Xi_{22}^{-1} \Xi_{21} - \Xi_{31}^T \Xi_{33}^{-1} \Xi_{31} - \Xi_{41}^T \Xi_{44}^{-1} \Xi_{41} - X^T \Psi^{-1} X < 0 \quad (38)$$

where

$$\Xi_{11} = \begin{bmatrix} \tilde{\Xi}_{11} & * & * & * & * & * & * \\ Q_1 - P_4 - 2Q_1 & * & * & * & * & * & * \\ Q_2 & 0 & -P_5 - 2Q_2 & * & * & * & * \\ Q_3 & 0 & 0 & -P_6 - 2Q_3 & * & * & * \\ 0 & Q_1 & 0 & 0 & -P_1 - Q_1 & * & * \\ 0 & 0 & Q_2 & 0 & 0 & -P_2 - Q_2 & * \\ 0 & 0 & 0 & Q_3 & 0 & 0 & -P_3 - Q_3 \end{bmatrix},$$

$$\tilde{\Xi}_{11} = -R_{acm} + P_1 + P_2 + P_3 + (\phi_M + 2)P_4 + (\varphi_M + 2)P_5 + (\psi_M + 2)P_6 - Q_1 - Q_2 - Q_3,$$

$$\Xi_{21} = \phi_M X, \quad \Xi_{31} = \varphi_M X, \quad \Xi_{41} = \psi_M X,$$

$$\Xi_{22} = \text{diag}\{-Q_1^{-1} - Q_1^{-1} - Q_1^{-1}\},$$

$$\Xi_{33} = \text{diag}\{-Q_2^{-1} - Q_2^{-1} - Q_2^{-1}\},$$

$$\Xi_{44} = \text{diag}\{-Q_3^{-1} - Q_3^{-1} - Q_3^{-1}\}, \quad \Psi = \text{diag}\{-\bar{R}_{bdn}^{-1} \cdots -\bar{R}_{bdn}^{-1}\},$$

$$X = \begin{bmatrix} (\bar{A} - I) \bar{\alpha}_1 I \bar{L} \bar{C} & \bar{B} K I_2 & \bar{\beta} \hat{B} K I_3 & 0 & 0 & 0 \\ 0 & \alpha_1 I_1 \bar{L} \bar{C} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \beta_1 \hat{B} K I_3 & 0 & 0 \end{bmatrix}.$$

By using the Schur Complement, (38) can be written as (39).

$$\begin{aligned} \Gamma &= \Xi + \bar{\eta}_1^T \bar{R}_{bdn} \bar{\eta}_1 + \bar{\eta}_2^T \bar{R}_{bdn} \bar{\eta}_2 + \bar{\eta}_3^T \bar{R}_{bdn} \bar{\eta}_3 \\ &= (\mu\nu\sigma + \mu\bar{\nu}\bar{\sigma} + \mu\nu\bar{\sigma} + \mu\bar{\nu}\bar{\sigma} + \bar{\mu}\nu\sigma + \bar{\mu}\nu\bar{\sigma} + \bar{\mu}\bar{\nu}\sigma + \bar{\mu}\bar{\nu}\bar{\sigma})\Xi \\ &\quad + \bar{\eta}_1^T \bar{R}_{bdn} \bar{\eta}_1 + \bar{\eta}_2^T \bar{R}_{bdn} \bar{\eta}_2 + \bar{\eta}_3^T \bar{R}_{bdn} \bar{\eta}_3 \\ &= \mu\nu\sigma \tilde{\Xi} + \bar{\nu}(\mu\sigma \tilde{\Xi}) + \bar{\sigma}(\mu\nu \tilde{\Xi}) + \bar{\nu}\bar{\sigma}(\mu \tilde{\Xi}) + \bar{\mu}(\nu\sigma \tilde{\Xi}) \\ &\quad + \bar{\mu}\bar{\sigma}(\bar{\nu} \tilde{\Xi}) + \bar{\mu}\bar{\nu}(\sigma \tilde{\Xi}) + \bar{\mu}\bar{\nu}\bar{\sigma} \tilde{\Xi} < 0 \end{aligned} \quad (39)$$

where

$$\tilde{\Xi} = \Xi + \bar{\eta}_1^T R_{bdn} \bar{\eta}_1 + \bar{\eta}_2^T R_{bdn} \bar{\eta}_2 + \bar{\eta}_3^T R_{bdn} \bar{\eta}_3,$$

$$\Xi = \begin{bmatrix} \Xi_{11} & * & * & * \\ \Xi_{21} & \Xi_{22} & * & * \\ \Xi_{31} & 0 & \Xi_{33} & * \\ \Xi_{41} & 0 & 0 & \Xi_{44} \end{bmatrix},$$

$$\bar{\eta}_1 = [\eta_1 \ 0 \ 0 \ 0], \quad \bar{\eta}_2 = [\eta_2 \ 0 \ 0 \ 0], \quad \bar{\eta}_3 = [\eta_3 \ 0 \ 0 \ 0],$$

$$\eta_1 = [\bar{A} \ \bar{\alpha}_1 I \bar{L} \bar{C} \ \bar{B} K I_2 \ \bar{\beta} \hat{B} K I_3 \ 0 \ 0 \ 0],$$

$$\eta_2 = [0 \ \alpha_1 I_1 \bar{L} \bar{C} \ 0 \ 0 \ 0 \ 0 \ 0],$$

$$\eta_3 = [0 \ 0 \ 0 \ \beta_1 \hat{B} K I_3 \ 0 \ 0 \ 0],$$

$$\mu = \sum_{b \in \Omega_k^a} \mu_{ab}, \quad \bar{\mu} = \sum_{b \in \Omega_{uk}^a} \mu_{ab}, \quad \nu = \sum_{d \in \Lambda_k^c} \nu_{cd},$$

$$\bar{\nu} = \sum_{d \in \Lambda_{uk}^c} \nu_{cd}, \quad \sigma = \sum_{n \in \Upsilon_k^m} \sigma_{mn}, \quad \bar{\sigma} = \sum_{n \in \Upsilon_{uk}^m} \sigma_{mn}.$$

Let  $S_{bdn} = R_{bdn}^{-1}$ , and one can get (40) by using the Schur Complement again.

$$\begin{aligned} &\mu\nu\sigma \left( \Xi + \bar{\eta}_1^T R_{bdn} \bar{\eta}_1 + \bar{\eta}_2^T R_{bdn} \bar{\eta}_2 + \bar{\eta}_3^T R_{bdn} \bar{\eta}_3 \right) \\ &= \begin{bmatrix} \mu\nu\sigma \Xi & * \\ \tilde{X}_{\Omega_k^a\Lambda_k^c\Upsilon_k^m} & \Psi_{\Omega_k^a\Lambda_k^c\Upsilon_k^m} \end{bmatrix} < 0 \end{aligned} \quad (40)$$

where

$$\tilde{X}_{\Omega_k^a\Lambda_k^c\Upsilon_k^m} = \text{diag}\left\{ \tilde{\Psi}_{\Omega_k^a\Lambda_k^c\Upsilon_k^m}, \tilde{\Psi}_{\Omega_k^a\Lambda_k^c\Upsilon_k^m}, \tilde{\Psi}_{\Omega_k^a\Lambda_k^c\Upsilon_k^m} \right\},$$

$$\tilde{\Psi}_{\Omega_k^a\Lambda_k^c\Upsilon_k^m} = \text{diag}\{-S_{\Omega_1^a\Lambda_1^c\Upsilon_1^m} \cdots -S_{\Omega_p^a\Lambda_p^c\Upsilon_p^m}\},$$

$$\begin{aligned} X_{\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T &= [\tilde{X}_{1\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T \tilde{X}_{2\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T \tilde{X}_{3\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T], \\ \tilde{X}_{1\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T &= [\sqrt{\mu_a \Omega_1^a \nu_c \Lambda_1^c \sigma_m \Upsilon_1^m \tilde{\eta}_1^T} \cdots \sqrt{\mu_a \Omega_p^a \nu_c \Lambda_r^c \sigma_m \Upsilon_r^m \tilde{\eta}_1^T}], \\ \tilde{X}_{2\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T &= [\sqrt{\mu_a \Omega_1^a \nu_c \Lambda_1^c \sigma_m \Upsilon_1^m \tilde{\eta}_2^T} \cdots \sqrt{\mu_a \Omega_p^a \nu_c \Lambda_r^c \sigma_m \Upsilon_r^m \tilde{\eta}_2^T}], \\ \tilde{X}_{3\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T &= [\sqrt{\mu_a \Omega_1^a \nu_c \Lambda_1^c \sigma_m \Upsilon_1^m \tilde{\eta}_3^T} \cdots \sqrt{\mu_a \Omega_p^a \nu_c \Lambda_r^c \sigma_m \Upsilon_r^m \tilde{\eta}_3^T}]. \end{aligned}$$

By substituting  $\tilde{A} = \tilde{A}_0 + \tilde{D}_1 \tilde{F}_1 \tilde{E}_1$ ,  $\tilde{B} = \tilde{B}_0 + \tilde{D}_2 \tilde{F}_2 \tilde{E}_2$ ,  $\tilde{C} = \tilde{C}_0 + \tilde{D}_3 \tilde{F}_3 \tilde{E}_3$  into (40), it can be decomposed into the certain part and the uncertain part. According Lemma 2, we have

$$\begin{aligned} \begin{bmatrix} \mu \nu \sigma \Xi & * \\ \tilde{X}_{\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T \Psi_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} & * \end{bmatrix} &= \begin{bmatrix} \mu \nu \sigma \tilde{\Xi}_0 & * \\ X_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} \Psi_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} & * \end{bmatrix} \\ &+ D_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} F E_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} + E_{\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T D_{\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T \\ &\leq \begin{bmatrix} \mu \nu \sigma \tilde{\Xi}_0 & * \\ X_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} \Psi_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} & * \end{bmatrix} + \varepsilon_1 D_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} D_{\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T \\ &+ \varepsilon_1^{-1} E N_{\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T E_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} \end{aligned} \quad (41)$$

or equivalently

$$\begin{bmatrix} \mu \nu \sigma \tilde{\Xi}_0 & * & * & * & * & * \\ X_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} \Psi_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} & * & * & * & * & * \\ \varepsilon_1 \tilde{D}^T & 0 & -\varepsilon_1 I & * & * & * \\ 0 & \varepsilon_1 \tilde{D}^T & 0 & -\varepsilon_1 I & * & * \\ \tilde{E} & 0 & 0 & 0 & -\varepsilon_1 I & * \\ \tilde{E}_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} & 0 & 0 & 0 & 0 & -\varepsilon_1 I \end{bmatrix} < 0 \quad (42)$$

where the definition of parameters in (41) is given in Appendix B.

The matrix inequality in (42) still contains  $Q_1, Q_1^{-1}, Q_2, Q_2^{-1}, Q_3, Q_3^{-1}$ . To convert (42) into LMI (30), the inequality  $-Q_1^{-1} < -2I + Q_1$  is used since  $(I - X_1^{-1})(I - X_1^{-1}) > 0 \Leftrightarrow -X_1^{-1} < -2I + X_1$  [55], so we can get (43).

$$\begin{aligned} \Xi_0 &= \begin{bmatrix} \Xi_{11} & * & * & * \\ \Xi_{210} & \tilde{\Xi}_{22} & * & * \\ \Xi_{310} & 0 & \tilde{\Xi}_{33} & * \\ \Xi_{410} & 0 & 0 & \tilde{\Xi}_{44} \end{bmatrix}, \\ \tilde{\Xi}_{22} &= \text{diag} \{ -2I + Q_1 \ -2I + Q_1 \ -2I + Q_1 \}, \\ \tilde{\Xi}_{33} &= \text{diag} \{ -2I + Q_2 \ -2I + Q_2 \ -2I + Q_2 \}, \\ \tilde{\Xi}_{44} &= \text{diag} \{ -2I + Q_3 \ -2I + Q_3 \ -2I + Q_3 \}. \end{aligned} \quad (43)$$

Since  $\mu_{ab} > 0, \nu_{cd} > 0, \sigma_{mn} > 0$ , if (30) - (37) hold, then (19) holds, that is, the closed-loop system (13) is stochastically stable. This ends the proof.

**V. SIMULATION ANALYSIS**

In this section, the effectiveness and generalization performance of the cloud controller designed in this paper are verified through simulation experiments of typical plants.

**A. EFFECTIVENESS OF THE CLOUD CONTROLLER**

*Example 1:* Consider the interval controlled plant with the following parameters:

$$\begin{aligned} A_1 &= \begin{bmatrix} [0.42, 0.62] & [-0.79, -0.59] \\ [-0.1, 0.1] & [0.09, 0.29] \end{bmatrix}, \quad B_1 = \begin{bmatrix} [0.2, 0.4] \\ [0.1, 0.3] \end{bmatrix}, \\ C &= \begin{bmatrix} 1.5 & 0.7 \\ 0.2 & 0.4 \end{bmatrix}, \end{aligned}$$

where the coefficients of the nominal system are

$$A_0 = \begin{bmatrix} 0.52 & -0.69 \\ 0 & 0.19 \end{bmatrix}, \quad B_0 = \begin{bmatrix} 0.3 \\ 0.2 \end{bmatrix}, \quad C = \begin{bmatrix} 1.5 & 0.7 \\ 0.2 & 0.4 \end{bmatrix}.$$

Assume feedback channel time-delay  $\tau_k^{sc} \in \Omega = \{0, 1\}$ , forward channel time-delay  $\tau_k^{ca} \in \tilde{\Upsilon} = \{0, 1\}$  and cloud controller time-delay  $\tau_k^c \in \Lambda = \{0, 1\}$ , and the transition probability matrices of which are as follows:

$$\Pi_{sc} = \begin{bmatrix} 0.8 & 0.2 \\ ? & ? \end{bmatrix}, \quad \Pi_{ca} = \begin{bmatrix} ? & ? \\ 0.7 & 0.3 \end{bmatrix}, \quad \Pi_c = \begin{bmatrix} 0.8 & 0.2 \\ ? & ? \end{bmatrix}.$$

The sum of forward channel time-delay and cloud controller time-delay is  $\psi_k \in \Upsilon = \{0, 1, 2\}$ , and the transition probability matrix of which is

$$\Pi_{ca+c} = \begin{bmatrix} ? & ? & ? \\ 0.56 & 0.38 & 0.06 \\ ? & ? & ? \end{bmatrix}.$$

The packet loss probability is  $1 - E\{\alpha_k\} = 1 - \bar{\alpha} = 1 - E\{\beta_k\} = 1 - \bar{\beta} = 0.2$ . Assuming that the observer parameters are uncertain, take them as the interval values whose midpoint values are the same as the ones of the corresponding coefficients of the controlled plant, but the widths are different, that is,

$$A_2 = \begin{bmatrix} [0.47, 0.57] & [-0.74, -0.64] \\ [-0.05, 0.05] & [0.14, 0.24] \end{bmatrix}, \quad B_2 = \begin{bmatrix} [0.25, 0.35] \\ [0.15, 0.25] \end{bmatrix}.$$

By using the MATLAB LMI toolbox, the control law gain matrix and observer gain matrix of the cloud controller considering the uncertainties existing in the cloud, network, and controlled plant can be obtained as

$$K = [0.0017 \ 0.0042], \quad L = \begin{bmatrix} 0.0068 & 0.0012 \\ -0.0082 & 0.0362 \end{bmatrix}.$$

The initial state of the system is  $x_0^T = [1 \ -0.5]^T$ . The distributions of  $\tau_k^{sc}, \tau_k^c, \tau_k^{ca}$  are shown in Figs. 4-6, respectively. The distributions of  $\alpha_k$ , and  $\beta_k$  are shown in Fig. 7 and Fig. 8, respectively. The state response curves under the control of the designed cloud controller in this paper are shown in Fig. 9.

It can be seen that the state response curves of CCS using the proposed cloud controller converge. This means that the cloud controller can effectively compensate for the impact of various uncertainties and keep the system stable, which demonstrates the effectiveness of the proposed cloud controller.

*Example 2:* Consider the interval controlled plant with the following parameters:

$$A_1 = \begin{bmatrix} [-0.74, -0.66] & [-0.13, -0.07] \\ [0.95, 1.05] & [0.19, 0.21] \end{bmatrix},$$

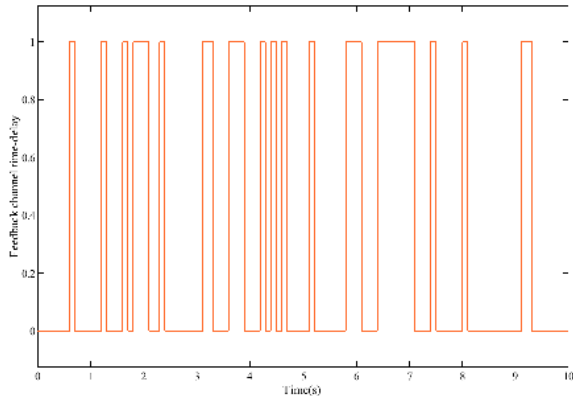


FIGURE 4. Distribution of  $\tau_k^{sc}$ .

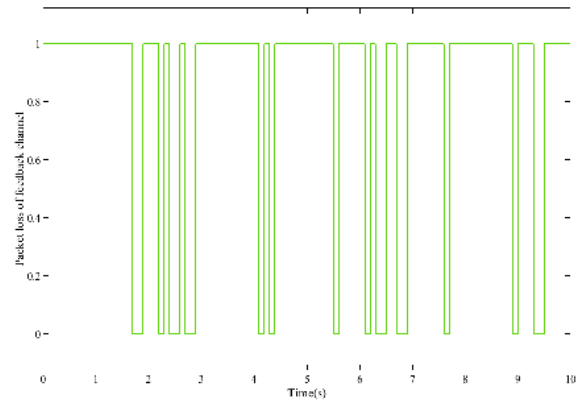


FIGURE 7. Distribution of  $\alpha_k$ .

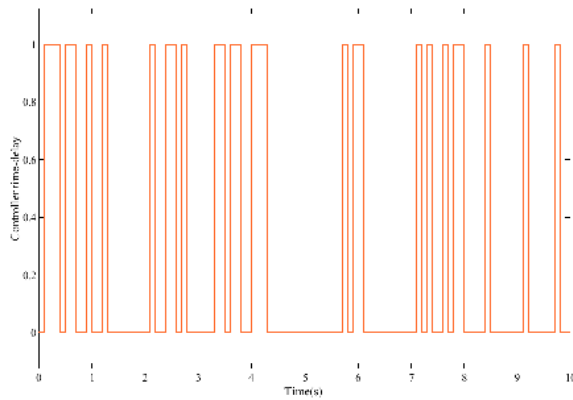


FIGURE 5. Distribution of  $\tau_k^c$ .

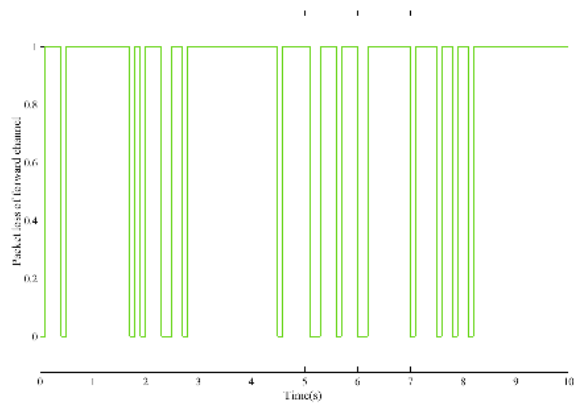


FIGURE 8. Distribution of  $\beta_k$ .

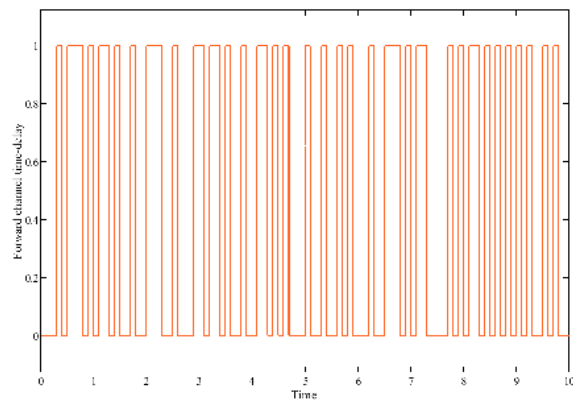


FIGURE 6. Distribution of  $\tau_k^{ca}$ .

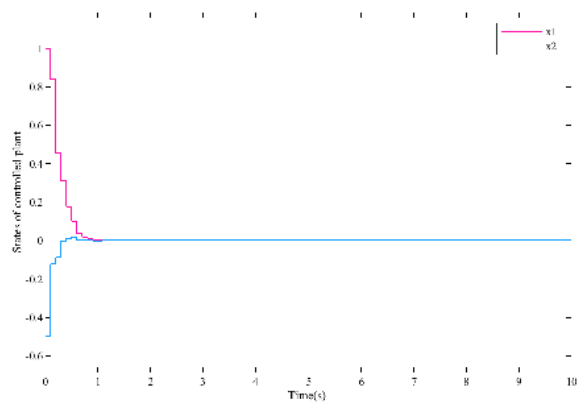


FIGURE 9. State response of the CCS using the proposed cloud controller.

$$B_1 = \begin{bmatrix} [1.8, 2.2] \\ [0.49, 0.51] \end{bmatrix},$$

$$C = [1 \ 0],$$

Obviously, the nominal system is unstable. Assume feedback channel time-delay  $\tau_k^{sc} \in \Omega = \{0, 1\}$ , forward channel time-delay  $\tau_k^{ca} \in \tilde{\Upsilon} = \{0, 1\}$  and cloud controller time-delay  $\tau_k^c \in \Lambda = \{0, 1\}$ , and the transition probability matrices of which are as follows:

$$\Pi_{sc} = \begin{bmatrix} 0.7 & 0.3 \\ ? & ? \end{bmatrix}, \quad \Pi_{ca} = \begin{bmatrix} ? & ? \\ 0.9 & 0.1 \end{bmatrix}, \quad \Pi_c = \begin{bmatrix} 0.7 & 0.3 \\ ? & ? \end{bmatrix}.$$

The sum of forward channel time-delay and cloud controller time-delay is  $\psi_k \in \Upsilon = \{0, 1, 2\}$ , and the transition probability matrix of which is

$$\Pi_{ca+c} = \begin{bmatrix} ? & ? & ? \\ 0.63 & 0.34 & 0.03 \\ ? & ? & ? \end{bmatrix}.$$

The packet loss probability is  $1 - E\{\alpha_k\} = 1 - \bar{\alpha} = 1 - E\{\beta_k\} = 1 - \bar{\beta} = 0.2$ . Assuming that the observer parameters are uncertain, take them as the interval values, that

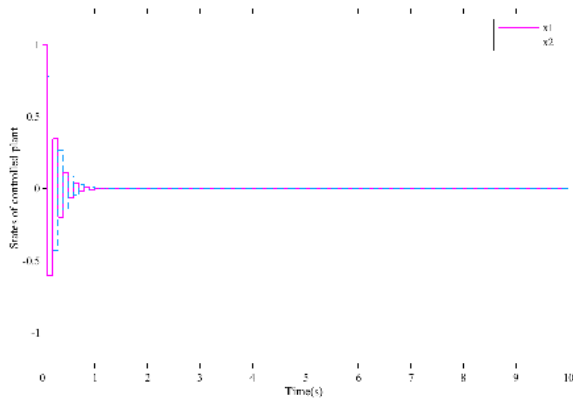


FIGURE 10. State response of the CCS using the proposed cloud controller.

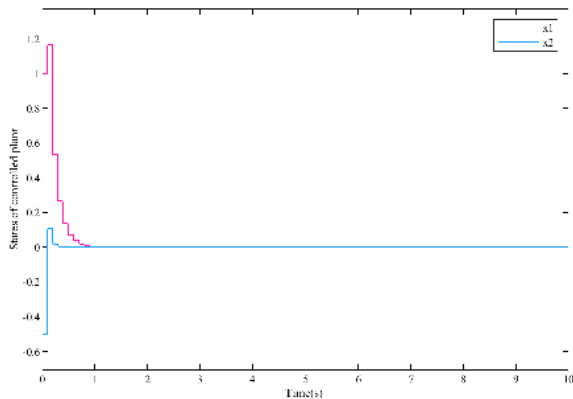


FIGURE 11. State response of the NCS using the proposed cloud controller.

is,

$$A_2 = \begin{bmatrix} [-0.75, -0.65] & [-0.15, -0.05] \\ [0.95, 1.05] & [0.15, 0.25] \end{bmatrix},$$

$$B_2 = \begin{bmatrix} [1.95, 2.05] \\ [0.45, 0.55] \end{bmatrix}.$$

According to Theorem 2, the control law gain matrix and observer gain matrix considering the uncertainties existing in the cloud, network, and controlled plant can be obtained as

$$K = [0.0010 \ 0.0001], \quad L = \begin{bmatrix} 0.0283 \\ -0.0271 \end{bmatrix}.$$

The initial state of the system is  $x_0^T = [1 \ -1]^T$ . The state response curves under the control of the designed cloud controller in this paper are shown in Fig. 10.

It can be seen that the state response curves of CCS using the proposed cloud controller converge. The cloud controller can keep the system stable, which demonstrates the effectiveness of the proposed cloud controller.

**B. GENERALIZATION PERFORMANCE OF THE CLOUD CONTROLLER**

The design of the cloud controller considers the uncertainty existing in the controlled plant, network channel, and controller, so it is not only applicable to the CCS but also

applicable to conventional control systems with uncertain controlled plants and the NCS with uncertain controlled plants or network time-delay and packet loss.

For example, when the cloud controller is applied to the NCS with bilateral time-delay and packet loss of network channel, the system state curves can be obtained, as shown in Fig. 11. It can be seen that the system state curves converge and the system keeps stable, which shows the generalization performance of the cloud controller.

**VI. CONCLUSION**

This paper proposes a new structure framework of the CCS. The system uncertainty is decomposed reasonably, through in-depth analysis of the internal characteristics of the CCS. System modeling is carried out from the control point of view, and the cloud controller is designed by utilizing the Lyapunov stability theorem and LMI method to compensate for or eliminate the impact of all the uncertainties existing in the cloud computing, the network, and the controlled plant. Simulation experiments demonstrate the effectiveness and generalization performance of the cloud controller.

The approach of CCS modeling and controller design proposed in this paper is actually a generalized control system design method. Considering that the deterministic system is a special case of uncertain systems, the proposed structure can also be called a general framework of control system design, which is suitable for designing the controller of a general system based on the stability principle.

In fact, the theory and application research of the CCS is still in a preliminary stage and is facing many difficulties and challenges. The complex characteristics of the cloud, network, and controlled plant need to be further considered. For example, the security of the cloud, the different stochastic characteristics of network and cloud and the coupling between them, and the nonlinear characteristics of the controlled plants need to be studied in the future. In addition, although the cloud controller can be successfully applied to the slow time-varying control system [56], it is also one of the future research directions to apply the cloud controller to the fast time-varying system in the actual environment.

**APPENDIX A  
PROOF OF THE THEOREM 1**

Let  $\zeta_k = \xi_{k+1} - \xi_k$ , and for the closed-loop system (13), we choose the Lyapunov-Krasovskii function as

$$V_k = \sum_{l=1}^4 V_l(\xi_k, \phi_k, \varphi_k, \psi_k) \triangleq \xi_k^T \Phi_{\phi_k, \varphi_k, \psi_k} \xi_k \quad (20)$$

where

$$V_1(\xi_k, \phi_k, \varphi_k, \psi_k) = \xi_k^T R_{\phi_k, \varphi_k, \psi_k} \xi_k$$

$$V_2(\xi_k, \phi_k, \varphi_k, \psi_k) = \sum_{\rho=k-\phi_M}^{k-1} \xi_\rho^T P_1 \xi_\rho + \sum_{\rho=k-\varphi_M}^{k-1} \xi_\rho^T P_2 \xi_\rho$$

$$+ \sum_{\rho=k-\psi_M}^{k-1} \xi_\rho^T P_3 \xi_\rho$$

$$\begin{aligned}
 V_3(\xi_k, \phi_k, \varphi_k, \psi_k) &= \sum_{j=-\phi_M+1}^0 \sum_{i=k+j-1}^{k-1} \xi_i^T P_4 \xi_i \\
 &+ \sum_{\rho=k-\phi_k}^{k-1} \xi_\rho^T P_4 \xi_\rho + \sum_{j=-\varphi_M+1}^0 \sum_{i=k+j-1}^{k-1} \\
 &\times \xi_i^T P_5 \xi_i + \sum_{\rho=k-\varphi_k}^{k-1} \xi_\rho^T P_5 \xi_\rho \\
 &+ \sum_{j=-\psi_M+1}^0 \sum_{i=k+j-1}^{k-1} \xi_i^T P_6 \xi_i \\
 &\sum_{\rho=k-\psi_k}^{k-1} \xi_\rho^T P_6 \xi_\rho \\
 V_4(\xi_k, \phi_k, \varphi_k, \psi_k) &= \sum_{j=-\phi_M+1}^0 \sum_{i=k+j-1}^{k-1} \phi_M \zeta_i^T Q_1 \zeta_i \\
 &+ \sum_{j=-\varphi_M+1}^0 \sum_{i=k+j-1}^{k-1} \varphi_M \zeta_i^T Q_2 \zeta_i \\
 &+ \sum_{j=-\psi_M+1}^0 \sum_{i=k+j-1}^{k-1} \psi_M \zeta_i^T Q_3 \zeta_i.
 \end{aligned}$$

Obviously, we have  $\Phi_{\phi_k, \varphi_k, \psi_k} > 0$ . By using the Bernoulli distribution properties stated in (1), one can get (21).

$$\begin{aligned}
 E\{\Delta V_1(\xi_k, \phi_k, \varphi_k, \psi_k)\} &= E\{\xi_{k+1}^T R_{\phi_{k+1}, \varphi_{k+1}, \psi_{k+1}} \xi_{k+1} \mid \phi_k = a, \varphi_k = c, \psi_k = m\} \\
 &- \xi_k^T R_{\phi_k, \varphi_k, \psi_k} \xi_k \\
 &= E\{(\tilde{A}\xi_k + (\alpha_k - \bar{\alpha})I_1 L\tilde{C}\xi_{k-\phi_k} + \bar{\alpha}I_1 L\tilde{C}\xi_{k-\phi_k} \\
 &+ \tilde{B}K I_2 \xi_{k-\varphi_k} + (\beta_k - \bar{\beta})\tilde{B}K I_3 \xi_{k-\psi_k} \\
 &+ \tilde{\beta}\tilde{B}K I_3 \xi_{k-\psi_k})^T \sum_{b=0}^{\phi_M} \sum_{d=0}^{\varphi_M} \sum_{n=0}^{\psi_M} \mu_{ab} \nu_{cd} \sigma_{mn} R_{bdn} (\tilde{A}\xi_k \\
 &+ (\alpha_k - \bar{\alpha})I_1 L\tilde{C}\xi_{k-\phi_k} + \bar{\alpha}I_1 L\tilde{C}\xi_{k-\phi_k} + \tilde{B}K I_2 \xi_{k-\varphi_k} \\
 &+ (\beta_k - \bar{\beta})\tilde{B}K I_3 \xi_{k-\psi_k} + \tilde{\beta}\tilde{B}K I_3 \xi_{k-\psi_k})\} - \xi_k^T R_{acm} \xi_k \\
 &= \xi_k^T \tilde{A}^T \tilde{R}_{bdn} \tilde{A} \xi_k + \xi_k^T \tilde{A}^T \tilde{R}_{bdn} \bar{\alpha} I_1 L \tilde{C} \xi_{k-\phi_k} \\
 &+ \xi_k^T \tilde{A}^T \tilde{R}_{bdn} \tilde{B} K I_2 \xi_{k-\varphi_k} + \xi_k^T \tilde{A}^T \tilde{R}_{bdn} \tilde{\beta} \tilde{B} K I_3 \xi_{k-\psi_k} \\
 &+ \alpha_1^2 \xi_{k-\phi_k}^T (I_1 L \tilde{C})^T \tilde{R}_{bdn} I_1 L \tilde{C} \xi_{k-\phi_k} \\
 &+ \xi_{k-\phi_k}^T (\bar{\alpha} I_1 L \tilde{C})^T \tilde{R}_{bdn} \tilde{A} \xi_k \\
 &+ \xi_{k-\phi_k}^T (\bar{\alpha} I_1 L \tilde{C})^T \tilde{R}_{bdn} \bar{\alpha} I_1 L \tilde{C} \xi_{k-\phi_k} \\
 &+ \xi_{k-\phi_k}^T (\bar{\alpha} I_1 L \tilde{C})^T \tilde{R}_{bdn} \tilde{B} K I_2 \xi_{k-\varphi_k} \\
 &+ \xi_{k-\phi_k}^T (\bar{\alpha} I_1 L \tilde{C})^T \tilde{R}_{bdn} \tilde{\beta} \tilde{B} K I_3 \xi_{k-\psi_k} \\
 &+ \xi_{k-\varphi_k}^T (\tilde{B} K I_2)^T \tilde{R}_{bdn} \tilde{A} \xi_k \\
 &+ \xi_{k-\varphi_k}^T (\tilde{B} K I_2)^T \tilde{R}_{bdn} \bar{\alpha} I_1 L \tilde{C} \xi_{k-\phi_k} \\
 &+ \xi_{k-\varphi_k}^T (\tilde{B} K I_2)^T \tilde{R}_{bdn} \tilde{B} K I_2 \xi_{k-\varphi_k} \\
 &+ \xi_{k-\varphi_k}^T (\tilde{B} K I_2)^T \tilde{R}_{bdn} \tilde{\beta} \tilde{B} K I_3 \xi_{k-\psi_k} \\
 &+ \beta_1^2 \xi_{k-\psi_k}^T (\tilde{B} K I_3)^T \tilde{R}_{bdn} \tilde{B} K I_3 \xi_{k-\psi_k}
 \end{aligned}$$

$$\begin{aligned}
 &+ \xi_{k-\psi_k}^T (\tilde{\beta} \tilde{B} K I_3)^T \tilde{R}_{bdn} \tilde{A} \xi_k \\
 &+ \xi_{k-\psi_k}^T (\tilde{\beta} \tilde{B} K I_3)^T \tilde{R}_{bdn} \bar{\alpha} I_1 L \tilde{C} \xi_{k-\phi_k} \\
 &+ \xi_{k-\psi_k}^T (\tilde{\beta} \tilde{B} K I_3)^T \tilde{R}_{bdn} \tilde{B} K I_2 \xi_{k-\varphi_k} \\
 &+ \xi_{k-\psi_k}^T (\tilde{\beta} \tilde{B} K I_3)^T \tilde{R}_{bdn} \tilde{\beta} \tilde{B} K I_3 \xi_{k-\psi_k} - \xi_k^T R_{acm} \xi_k \quad (21)
 \end{aligned}$$

$$\begin{aligned}
 E\{\Delta V_2(\xi_k, \phi_k, \varphi_k, \psi_k)\} &= \xi_k^T P_1 \xi_k - \xi_{k-\phi_M}^T P_1 \xi_{k-\phi_M} \\
 &+ \xi_k^T P_2 \xi_k - \xi_{k-\varphi_M}^T P_2 \xi_{k-\varphi_M} + \xi_k^T P_3 \xi_k - \xi_{k-\psi_M}^T P_3 \xi_{k-\psi_M} \quad (22)
 \end{aligned}$$

$$\begin{aligned}
 E\{\Delta V_3(\xi_k, \phi_k, \varphi_k, \psi_k)\} &= \phi_M \xi_k^T P_4 \xi_k - \sum_{\rho=k-\phi_M}^{k-1} \xi_\rho^T P_4 \xi_\rho + \sum_{\rho=k+1-\phi_{k+1}}^k \xi_\rho^T P_4 \xi_\rho \\
 &- \sum_{\rho=k-\phi_k}^{k-1} \xi_\rho^T P_4 \xi_\rho + \varphi_M \xi_k^T P_5 \xi_k - \sum_{\rho=k-\varphi_M}^{k-1} \xi_\rho^T P_5 \xi_\rho \\
 &+ \sum_{\rho=k+1-\varphi_{k+1}}^k \xi_\rho^T P_5 \xi_\rho - \sum_{\rho=k-\varphi_k}^{k-1} \xi_\rho^T P_5 \xi_\rho + \psi_M \xi_k^T P_6 \xi_k \\
 &- \sum_{\rho=k-\psi_M}^{k-1} \xi_\rho^T P_6 \xi_\rho + \sum_{\rho=k+1-\psi_{k+1}}^k \xi_\rho^T P_6 \xi_\rho - \sum_{\rho=k-\psi_k}^{k-1} \xi_\rho^T P_6 \xi_\rho \quad (23)
 \end{aligned}$$

Since

$$\begin{aligned}
 &- \sum_{\rho=k-\phi_M}^{k-1} \xi_\rho^T P_4 \xi_\rho + \sum_{\rho=k+1-\phi_{k+1}}^k \xi_\rho^T P_4 \xi_\rho - \sum_{\rho=k-\phi_k}^{k-1} \xi_\rho^T P_4 \xi_\rho \\
 &= - \sum_{\rho=k-\phi_M}^{k-1} \xi_\rho^T P_4 \xi_\rho + \xi_k^T P_4 \xi_k - \xi_{k-\phi_k}^T P_4 \xi_{k-\phi_k} \\
 &+ \sum_{\rho=k+1-\phi_{k+1}}^k \xi_\rho^T P_4 \xi_\rho + \sum_{\rho=k+1-\phi_k}^{k-1} \xi_\rho^T P_4 \xi_\rho - \sum_{\rho=k+1-\phi_k}^{k-1} \xi_\rho^T P_4 \xi_\rho \\
 &\leq 2\xi_k^T P_4 \xi_k - \xi_{k-\phi_k}^T P_4 \xi_{k-\phi_k},
 \end{aligned}$$

one can obtain

$$\begin{aligned}
 E\{\Delta V_3(\xi_k, \phi_k, \varphi_k, \psi_k)\} &\leq (\phi_M + 2)\xi_k^T P_4 \xi_k \\
 &- \xi_{k-\phi_k}^T P_4 \xi_{k-\phi_k} + (\varphi_M + 2)\xi_k^T P_5 \xi_k - \xi_{k-\varphi_k}^T P_5 \xi_{k-\varphi_k} \\
 &+ (\psi_M + 2)\xi_k^T P_6 \xi_k - \xi_{k-\psi_k}^T P_6 \xi_{k-\psi_k} \quad (24)
 \end{aligned}$$

$$\begin{aligned}
 E\{\Delta V_4(\xi_k, \phi_k, \varphi_k, \psi_k)\} &= E\{\phi_M^2 \zeta_k^T Q_1 \zeta_k\} - \sum_{\rho=k-\phi_M}^{k-1} \phi_M \zeta_\rho^T Q_1 \zeta_\rho + E\{\varphi_M^2 \zeta_k^T Q_2 \zeta_k\} \\
 &- \sum_{\rho=k-\varphi_M}^{k-1} \varphi_M \zeta_\rho^T Q_2 \zeta_\rho + E\{\psi_M^2 \zeta_k^T Q_3 \zeta_k\} - \sum_{\rho=k-\psi_M}^{k-1} \psi_M \zeta_\rho^T Q_3 \zeta_\rho \quad (25)
 \end{aligned}$$

Note that

$$\begin{aligned}
 E\{\phi_M^2 \zeta_k^T Q_1 \zeta_k\} &= \phi_M^2 E\{((\tilde{A}-I)\xi_k + (\alpha_k - \bar{\alpha})I_1 L\tilde{C}\xi_{k-\phi_k} \\
 &+ \bar{\alpha}I_1 L\tilde{C}\xi_{k-\phi_k} + \tilde{B}K I_2 \xi_{k-\varphi_k} + (\beta_k - \bar{\beta})\tilde{B}K I_3 \xi_{k-\psi_k} \\
 &+ \tilde{\beta}\tilde{B}K I_3 \xi_{k-\psi_k})^T Q_1 ((\tilde{A}-I)\xi_k + (\alpha_k - \bar{\alpha})I_1 L\tilde{C}\xi_{k-\phi_k} \\
 &+ \bar{\alpha}I_1 L\tilde{C}\xi_{k-\phi_k} + \tilde{B}K I_2 \xi_{k-\varphi_k} + (\beta_k - \bar{\beta})\tilde{B}K I_3 \xi_{k-\psi_k} \\
 &+ \tilde{\beta}\tilde{B}K I_3 \xi_{k-\psi_k})\} \quad (26)
 \end{aligned}$$



$$\begin{aligned} \Psi_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m} &= \text{diag} \left\{ \tilde{\Psi}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m} \tilde{\Psi}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m} \tilde{\Psi}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m} \right\}, \\ \tilde{\Psi}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m} &= \text{diag} \{-S_{bd} \Upsilon_1^m \cdots -S_{bd} \Upsilon_1^m\}, \\ X_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m}^T &= \left[ \check{X}_{1\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m}^T \check{X}_{2\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m}^T \check{X}_{3\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m}^T \right], \\ \check{X}_{i\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m}^T &= [\sqrt{\sigma_m \Upsilon_1^m} \tilde{\eta}_i^T \cdots \sqrt{\sigma_m \Upsilon_1^m} \tilde{\eta}_i^T], \\ \tilde{D}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m} &= \text{diag} \left\{ \tilde{D}_{1\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m} \tilde{D}_{2\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m} \tilde{D}_{3\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m} \right\}, \\ \tilde{D}_{i\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m} &= \text{diag} \left\{ \sqrt{\sigma_m \Upsilon_1^m} \tilde{D}_i \cdots \sqrt{\sigma_m \Upsilon_1^m} \tilde{D}_i \right\}, \\ \tilde{E}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m}^T &= \left[ \tilde{E}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m}^T \tilde{E}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m}^T \tilde{E}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m}^T \right], \\ \tilde{E}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_k^m}^T &= [\sqrt{\sigma_m \Upsilon_1^m} \hat{E}^T \cdots \sqrt{\sigma_m \Upsilon_1^m} \hat{E}^T], \\ \Psi_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m} &= \text{diag} \left\{ \tilde{\Psi}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m} \tilde{\Psi}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m} \tilde{\Psi}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m} \right\}, \\ \tilde{\Psi}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m} &= \text{diag} \{-S_{bdn} \cdots -S_{bdn}\}, \\ X_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m}^T &= \left[ \check{X}_{1\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m}^T \check{X}_{2\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m}^T \check{X}_{3\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m}^T \right], \\ \check{X}_{i\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m}^T &= [\tilde{\eta}_i^T \cdots \tilde{\eta}_i^T], \\ \tilde{D}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m} &= \text{diag} \left\{ \tilde{D}_{1\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m} \tilde{D}_{2\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m} \tilde{D}_{3\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m} \right\}, \\ \tilde{D}_{i\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m} &= \text{diag} \{\tilde{D}_i \cdots \tilde{D}_i\}, (i = 1, 2, 3), \\ \tilde{E}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m}^T &= \left[ \tilde{E}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m}^T \tilde{E}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m}^T \tilde{E}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m}^T \right], \\ \tilde{E}_{\Omega_{uk}^a \Lambda_{uk}^c \Upsilon_{uk}^m}^T &= [\hat{E}^T \cdots \hat{E}^T], \end{aligned}$$

**B. DEFINITION OF PARAMETERS IN (41)**

$$\begin{aligned} \tilde{\Xi}_0 &= \begin{bmatrix} \Xi_{11} & * & * & * \\ \Xi_{210} & \Xi_{22} & * & * \\ \Xi_{310} & 0 & \Xi_{33} & * \\ \Xi_{410} & 0 & 0 & \Xi_{44} \end{bmatrix}, \\ \Xi_{210} &= \phi_M X_0, \quad \Xi_{310} = \varphi_M X_0, \quad \Xi_{410} = \psi_M X_0, \\ X_0 &= \begin{bmatrix} (\tilde{A} - I) \tilde{\alpha} I_1 L \tilde{C} & \tilde{B}_0 K I_2 & \tilde{\beta} \tilde{B}_0 K I_3 & 0 & 0 & 0 \\ 0 & \alpha_1 I_1 L \tilde{C} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \beta_1 \tilde{B}_0 K I_3 & 0 & 0 \end{bmatrix}, \\ X_{\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T &= \left[ \check{X}_{1\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T \check{X}_{2\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T \check{X}_{3\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T \right], \\ \check{X}_{i\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T &= [\sqrt{\mu_a \Omega_1^a \nu_c \Lambda_1^c \sigma_m \Upsilon_1^m} \tilde{\eta}_i^T \cdots \sqrt{\mu_a \Omega_p^a \nu_c \Lambda_p^c \sigma_m \Upsilon_1^m} \tilde{\eta}_i^T], \\ \tilde{\eta}_1 &= [\eta_{10} \ 0 \ 0 \ 0], \quad \tilde{\eta}_2 = [\eta_{20} \ 0 \ 0 \ 0], \\ \tilde{\eta}_3 &= [\eta_{30} \ 0 \ 0 \ 0], \\ \eta_{10} &= [\tilde{A} \ \tilde{\alpha} I_1 L \tilde{C} \ \tilde{B}_0 \ K I_2 \ \tilde{\beta} \tilde{B}_0 \ K I_3 \ 0 \ 0 \ 0], \\ \eta_{20} &= [0 \ \alpha_1 I_1 L \tilde{C} \ 0 \ 0 \ 0 \ 0 \ 0], \\ \eta_{30} &= [0 \ 0 \ 0 \ \beta_1 \tilde{B}_0 \ K I_3 \ 0 \ 0 \ 0]. \\ D_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} &= \begin{bmatrix} \tilde{D} & 0 \\ 0 & \tilde{D}_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} \end{bmatrix}, \\ \tilde{D} &= \text{diag} \{0, \phi_M \mu \nu \sigma \hat{D}, \varphi_M \mu \nu \sigma \hat{D}, \psi_M \mu \nu \sigma \hat{D}\}, \\ \hat{D} &= \begin{bmatrix} \tilde{D}_1 & \tilde{D}_2 & \tilde{\beta} \tilde{D}_3 \\ 0 & 0 & 0 \\ 0 & 0 & \beta_1 \tilde{D}_3 \end{bmatrix}, \end{aligned}$$

$$\begin{aligned} \tilde{D}_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} &= \text{diag} \left\{ \tilde{D}_{1\Omega_k^a \Lambda_k^c \Upsilon_k^m} \tilde{D}_{2\Omega_k^a \Lambda_k^c \Upsilon_k^m} \tilde{D}_{3\Omega_k^a \Lambda_k^c \Upsilon_k^m} \right\}, \\ \tilde{D}_{i\Omega_k^a \Lambda_k^c \Upsilon_k^m} &= \text{diag} \left\{ \sqrt{\mu_a \Omega_1^a \nu_c \Lambda_1^c \sigma_m \Upsilon_1^m} \tilde{D}_i \cdots \sqrt{\mu_a \Omega_p^a \nu_c \Lambda_p^c \sigma_m \Upsilon_1^m} \tilde{D}_i \right\}, \\ &(i = 1, 2, 3), \\ E_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} &= \begin{bmatrix} \tilde{E} & 0 \\ \tilde{E}_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} & 0 \end{bmatrix}, \quad \tilde{E}^T = [0 \ \hat{E}^T \ \hat{E}^T \ \hat{E}^T], \\ \hat{E} &= [\tilde{E} \ 0 \ 0 \ 0], \\ \tilde{E} &= \begin{bmatrix} \tilde{E}_1 \ 0 \ 0 & 0 & 0 \ 0 \ 0 \\ 0 \ 0 \ \tilde{E}_2 K I_2 & 0 & 0 \ 0 \ 0 \\ 0 \ 0 \ 0 & \tilde{E}_3 K I_3 & 0 \ 0 \ 0 \end{bmatrix}, \\ \tilde{E}_{\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T &= \left[ \tilde{E}_{\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T \tilde{E}_{\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T \tilde{E}_{\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T \right], \\ \tilde{E}_{\Omega_k^a \Lambda_k^c \Upsilon_k^m}^T &= [\sqrt{\mu_a \Omega_1^a \nu_c \Lambda_1^c \sigma_m \Upsilon_1^m} \hat{E}^T \cdots \sqrt{\mu_a \Omega_p^a \nu_c \Lambda_p^c \sigma_m \Upsilon_1^m} \hat{E}^T], \\ F &= \begin{bmatrix} \hat{F} & 0 \\ 0 & F_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} \end{bmatrix}, \quad \hat{F} = \text{diag} \{0, \tilde{F}, \tilde{F}, \tilde{F}\}, \\ F_{\Omega_k^a \Lambda_k^c \Upsilon_k^m} &= \text{diag} \left\{ \tilde{F} \cdots \tilde{F} \right\}, \quad \tilde{F} = \text{diag} \{ \tilde{F}_1 \ \tilde{F}_2 \ \tilde{F}_3 \}, \end{aligned}$$

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