

Fatigue, alcohol and performance impairment

Reduced opportunity for sleep and reduced sleep quality are frequently related to accidents involving shift-workers¹⁻³. Poor-quality sleep and inadequate recovery leads to increased fatigue, decreased alertness and impaired performance in a variety of cognitive psychomotor tests⁴. However, the risks associated with fatigue are not well quantified. Here we equate the performance impairment caused by fatigue with that due to alcohol intoxication, and show that moderate levels of fatigue produce higher levels of impairment than the proscribed level of alcohol intoxication.

Forty subjects participated in two counterbalanced experiments. In one they were kept awake for 28 hours (from 8:00 until 12:00 the following day), and in the other they were asked to consume 10–15 g alcohol at 30-min intervals from 8:00 until their mean blood alcohol concentration reached 0.10%. We measured cognitive psychomotor performance at half-hourly intervals using a computer-administered test of hand–eye coordination (an unpredictable tracking task). Results are expressed as a percentage

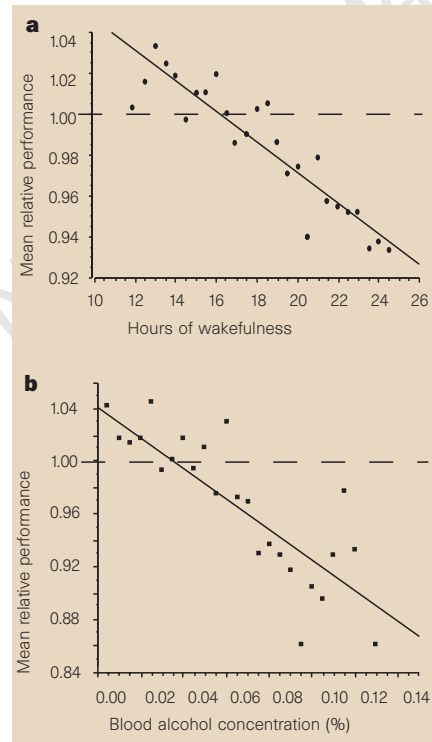


Figure 1 Scatter plot and linear regression of mean relative performance levels against: **a**, time, between the tenth and twenty-sixth hour of sustained wakefulness ($F_{1,24}=132.9$, $P<0.05$, $R^2=0.92$); and **b**, blood alcohol concentrations up to 0.13%, ($F_{1,24}=54.4$, $P<0.05$, $R^2=0.69$).

of performance at the start of the session.

Performance decreased significantly in both conditions. Between the tenth and twenty-sixth hours of wakefulness, mean relative performance on the tracking task decreased by 0.74% per hour. Regression analysis in the sustained wakefulness condition revealed a linear correlation between mean relative performance and hours of wakefulness that accounted for roughly 90% of the variance (Fig. 1a).

Regression analysis in the alcohol condition indicated a significant linear correlation between subject's mean blood alcohol concentration and mean relative performance that accounted for roughly 70% of the variance (Fig. 1b). For each 0.01% increase in blood alcohol, performance decreased by 1.16%. Thus, at a mean blood alcohol concentration of 0.10%, mean relative performance on the tracking task decreased, on average, by 11.6%.

Equating the two rates at which performance declined (percentage decline per hour of wakefulness and percentage decline with change in blood alcohol concentration), we calculated that the performance decrement for each hour of wakefulness between 10 and 26 hours was equivalent to the performance decrement observed with a 0.004% rise in blood alcohol concentration. Therefore, after 17 hours of sustained wakefulness (3:00) cognitive psychomotor performance decreased to a level equivalent to the performance impairment observed at a blood alcohol concentration of 0.05%. This is the proscribed level of alcohol intoxication in many western industrialized countries. After 24 hours of sustained wakefulness (8:00) cognitive psychomotor performance decreased to a level equivalent to the performance deficit observed at a blood alcohol concentration of roughly 0.10%.

Plotting mean relative performance and blood alcohol concentration 'equivalent' against hours of wakefulness (Fig. 2), it is clear that the effects of moderate sleep loss on performance are similar to moderate alcohol intoxication. As about 50% of shift-workers do not sleep on the day before the first night-shift⁵, and levels of fatigue on subsequent night-shifts can be even higher⁶, our data indicate that the performance impairment associated with shift-work could be even greater than reported here.

Our results underscore the fact that relatively moderate levels of fatigue impair performance to an extent equivalent to or greater than is currently acceptable for

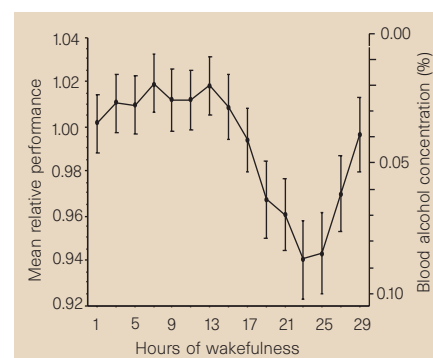


Figure 2 Performance in the sustained wakefulness condition expressed as mean relative performance and the percentage blood alcohol concentration equivalent. Error bars $\pm$ s.e.m.

alcohol intoxication. By expressing fatigue-related impairment as a 'blood-alcohol equivalent', we can provide policy-makers and the community with an easily grasped index of the relative impairment associated with fatigue.

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Entropy difference between crystal phases

In a recent Letter¹, Woodcock reported the results of a molecular dynamics study in which he claims to have finally determined the free-energy difference between the hexagonal close-packed (h.c.p.) and face-centred cubic (f.c.c.) phases of a crystal of (classical) hard spheres. Woodcock reports a small positive difference in the reduced Gibbs free-energy, which is equivalent to a difference in the reduced Helmholtz free-energy of $\Delta F^* \equiv (F_{h.c.p.} - F_{f.c.c.})/RT = 0.005(1)$ at the melting density (R is the gas constant, T is the absolute temperature, and the num-

ber in parentheses is the estimated error in the last digit). As Woodcock correctly points out, the calculation of the relative stability of the f.c.c. and h.c.p. phases of hard spheres is a long-standing problem in statistical physics. Attempts to resolve it date back to the work of Alder, Hoover and colleagues^{2–5}, and most recently, a direct simulation by Frenkel and Ladd⁶, obtaining the bounds of Helmholtz free-energy of $-0.001 \leq \Delta F \leq 0.002$. Woodcock's estimate is incompatible with this latter result.

To resolve this issue, we made accurate calculations of the free-energy difference between h.c.p. and f.c.c. hard-sphere crystals both at the melting density (73.6% of the density of regular close packing) and at close packing, using two different methods. We find that $\Delta F = 0.0009(2)$ at melting, a result that is quite consistent with the earlier work, but is five times smaller than Woodcock's estimate. Woodcock does not explain how he arrives at an error estimate of 20% — our work suggests that the numerical error in his result must have been four times larger than the entire h.c.p. – f.c.c. free-energy difference.

Nevertheless, we do agree with the sign of Woodcock's estimate — the f.c.c. crystal is indeed more stable than the h.c.p. crystal. This might explain the tendency towards f.c.c. packing seen in some experimental studies of hard-sphere colloids⁷. In one set of simulations, we used the 'Einstein-crystal' method^{6,8}, simulating crystals of 12,096 hard spheres (slightly larger than the largest system studied by Woodcock), and computed the Helmholtz free-energies of the two phases using a 20-point Gauss–Legendre quadrature. Every point in this quadrature involved a Monte Carlo simulation of 10^5 trial moves per particle, excluding equilibration. We find that the free-energy difference between h.c.p. and f.c.c. at melting is $\Delta F = 0.00087(20)$, and at close packing $\Delta F = 0.00094(30)$. The statistical error was computed on the basis of the variance in the block averages of the individual Monte Carlo runs⁹.

We also performed simulations using a new 'multi-hamiltonian' method (S.-C. M. and D. A. H., manuscript in preparation) that directly equilibrates the h.c.p. and f.c.c. hard-sphere crystals with each other by a set of intermediate states with different interactions but essentially the same free-energy. These latter simulations were done on much smaller samples (64 to 512 spheres) and obtained essentially the same free-energy differences (for 512 spheres, $\Delta F = 0.00085(10)$ near melting, and $0.0011(2)$ at close packing) as the 'Einstein-crystal' simulations, with comparable statistical errors. Statistically significant finite-size effects were detected only for the smallest size (64 spheres) near melting, where ΔF dropped to near zero.

In any event, our result for the f.c.c.–h.c.p. free-energy difference for large hard-sphere crystals at melting is much closer to $\Delta F = 0$, proposed almost 30 years ago by Alder and co-workers, than to the recent estimate by Woodcock.

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Woodcock replies — I reported the discovery a substantial area of pressure difference (ΔP) between the f.c.c. and h.c.p. single-occupancy-cell models, which arises from a difference in order–disorder transition pressures. The result was a free-energy difference in favour of f.c.c., corresponding to an entropy difference $0.005Nk_B$, over the range $V = 1.00N\sigma^3$ to $1.25N\sigma^3$, with a generous uncertainty (± 0.001), estimated by integrating the standard deviations of sub-averages of ΔP for individual data points. Extension of the computations on either side of the phase transition have since revealed a tail in the pressure difference for $V > 1.25N\sigma^3$ in favour of h.c.p. There is also a weak pressure difference for volumes below melting. I have now obtained more accurate data for these tails, including new data points on both sides of the single-occupancy-cell phase transition (Fig. 1).

I did not originally calculate the pressure difference in the stable crystal range, relying on earlier findings that ΔP up to melting was not detectable by molecular dynamics computation², and that these showed the two crystals to have indistinguishable crystal constants C_0 and C_1 (ref. 4). Consequently I assumed no difference between the Gibbs and Helmholtz free-energies in the stable

crystal range.

A detectable pressure difference between f.c.c. and h.c.p. crystals below melting, however, has now been computed, both by R. Speedy (personal communication) and myself. This small pressure difference means that the entropy difference at constant volume — which equals the Helmholtz free-energy difference for hard spheres — is not the same as the Gibbs free-energy difference, which determines the stable crystal structure at freezing. However, the correction is small, $\sim 0.000015Nk_B T$.

At the melting volume (V_m) of $0.96N\sigma^3$, I calculate the pressure difference to be $0.0030(5)k_B T/\sigma^3$ ($N = 12,000$). Alder *et al.*³ adopted too large a value for ΔP_m ($0.02k_B T/\sigma^3$), and further guessed wrongly that the absolute difference decreased linearly with density to zero at V_0 . In fact they estimated the Helmholtz free-energy difference ($\Delta F_m - \Delta F_0$) to be $0.002Nk_B T$ in favour of f.c.c. My data (Fig. 1) show that the pressure difference found at melting actually decreases to negligible values more rapidly, and that the change in free-energy difference between close packing and melting is of the order $0.0003Nk_B T$. The closeness of the result of Alder *et al.* to any of the present results, or indeed to zero, is therefore an irrelevance.

The Einstein-crystal method¹⁰ (used both by Frenkel and Ladd⁶ and here by Bolhuis and Frenkel), the multi-hamiltonian method and the Hoover–Ree single-occupancy-cell method, if accurately implemented, should all give the correct answer. I am still working on this problem, but the latest result for the Helmholtz free-energy difference between the h.c.p. and f.c.c. structures (f.c.c. having the lower free-energy) at close packing gives:

$$\Delta F_0 = \int_{V_0}^{\infty} (P_{\text{h.c.p.}} - P_{\text{f.c.c.}}) dV = 0.0026 \pm 0.001 Nk_B T.$$

The change in Helmholtz free-energy difference between close-packing and the melting volume amounts to only $0.0003(1)Nk_B T$, as shown by the tiny, positive area in $\Delta P(V)_T$ up to the melting volume (V_m) (see Fig. 1). Hence, the Helmholtz free-energy difference at the melting volume is $\Delta F_m = 0.0023(10)Nk_B T$. There remains a quantitative disagreement between my result and the other two methods, but my original conclusion that the f.c.c. phase is everywhere the more stable crystal phase for hard spheres is confirmed by all the new results. It is also gratifying that the result for the tiny free-energy difference between close packing and melting show a remarkable consistency, within the error bars, by all three methods.

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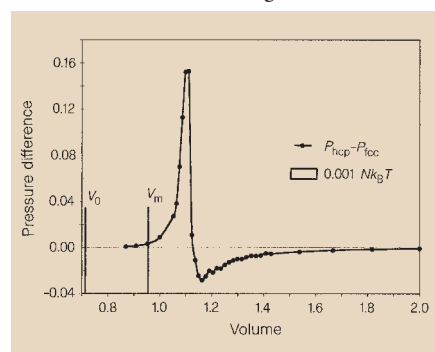


Figure 1 Latest molecular dynamic data for the pressure difference as a function of volume at constant temperature, $\Delta P(V)_T$, between the h.c.p. and f.c.c. single-occupancy-cell crystal structures for hard spheres; V_0 is the close-packed crystal volume and V_m is the volume at melting. The area under this curve is the Helmholtz free-energy difference between the two crystal structures at close packing in units of $Nk_B T$.

